# WORKSHOP PROGRAM

Combinatorial geometries: matroids, oriented matroids and applications

Géométries combinatoires : matroïdes, matroïdes orientés et applications



Ringel's arrangement

Marseille - Luminy, 2-6 April, 2013

Dedicated to the memory of Michel Las Vergnas

Organizing committee

Emeric GIOAN Jorge RAMIREZ ALFONSIN Scientific committee

Alexandre BOROVIK Raul CORDOVIL Michel LAS VERGNAS (R.I.P.) Jim LAWRENCE András RECSKI





Tuesday 2 at 9h:

# Radon Catalogs, the Odd-Even Invariant, and Valuations

Jim LAWRENCE

(George Mason University, USA)

Many numerical invariants of oriented matroids correspond to valuations on the lattice of closed subcomplexes of the associated cell complex. The odd-even invariant and the entries of the Radon catalog are such invariants. We will study this connection by, among other things, describing bases for the space of valuations, whose elements are derived from the Radon catalog or from the odd-even invariants.

Tuesday 2 at 9h45:

## Geometry of lopsided sets

Hans-Jürgen BANDELT

(Fachbereich Mathematik, Universität Hamburg)

Lopsided sets were introduced by Jim Lawrence in 1983 to encompass the intersection patterns of convex sets with the hyperorthants in Euclidean n-space. Lopsided sets were then characterized as the subsets of the discrete n-cube (of  $\pm 1$ -sequences of length n) for which the intersections with the n-cube faces are either the entire faces or empty or non-symmetric (i.e., not closed under the antipodal maps of the respective faces). In the eighties and nineties, lopsided sets were rediscovered in various disguises and alternatively named "simple", "ample", "extremal for (reverse) Sauer" or "shattering-extremal". Altogether we found more than two dozen equivalent descriptions of lopsidedness (Eur. J. Combin. 27, 2006, pp. 669-689); so, there would still be ample opportunity for future rediscoveries.

The geometric realization of lopsided sets as cubihedra endowed with the intrinsic 11 metric yields the appropriate "orthoconvex" subsets of the n-space from which the lopsided sets are exactly retrieved as the sign vectors codifying the intersection patterns with the hyperorthants. Moreover, the  $\pm 1,0$ -valued barycenter maps of the maximal hypercube constituents of lopsided sets determine the geometric features of the associated cubihedra and can be characterized in terms of axioms which largely overlap the standard axiom set for covectors (faces) of oriented matroids. This naturally leads to a common generalization of lopsided sets and oriented matroids as "conditional oriented matroids" which can be regarded as certain complexes of oriented matroids.

For the most part, joint work with Victor Chepoi, Andreas Dress, and Jack Koolen

## Between partial cubes and oriented matroids

#### Kolja KNAUER

(Technische Universität Berlin, Germany)

A graph is called a partial cube if it is an isometric subgraph of some hypercube. Many nice graphs are partial cubes, e.g., tope graphs of oriented matroids, graphs of lopsided sets, linear extension graphs of posets, diagrams of distributive lattices. Nevertheless the class of partial cubes seems to be too large to capture important features of these graphs.

We introduce 'conditional oriented matroids', which may be regarded as complexes of oriented matroids. Tope graphs of conditional oriented matroids form a tighter generalization of the above examples. We present several properties and discuss nice open problems.

Joint work with H.-J. Bandelt, V. Chepoi, M. Kovse, supported by ANR TEOMATRO

Tuesday 2 at 11h45:

## Tutte polynomials and topological representations of partial cubes

Matjaž KOVŠE

(University of Leipzig, Germany)

Partial cubes (isometric subgraphs of hypercubes) form a well studied class of graphs with nice metric properties. They appear in diverse areas, like: computer science, mathematical chemistry, mathematical biology, social sciences, psychology. In mathematics they appear, besides in graph theory and coùbinatorics, also in topology, algebra and computational geometry. Tope graphs of oriented matroids are examples of partial cubes. One of the fundamental results about oriented matroids is the topological representation theorem. Topological representation theorem for partial cubes will be discussed and topological representation theorem for planar partial cubes will be presented. Example of a partial cube which is not representable with pseudospheres will be also presented. Tutte polynomials of partial cubes, which generalize Tutte polynomials of hyperplane arrangements, as introduced by Ardila, will be also discussed.

Joint work with Kolja Knauer, Martin Milanic, Ferdinando Cicalese. This work was supported in part by the Deutsche Forschungsgemeinschaft within the EUROCORES Programme EUROGIGA (project GReGAS) of the European Science Foundation.

Tuesday 2 at 14h30:

## Double Permutation Sequences and Arrangements of Planar Families of Convex Sets with Applications

### Richard POLLACK

(New York University, USA)

We recall Permutation Sequences and Allowable Permutation Sequences and the Theorem that every Allowable permutation Sequence can be realized by an arrangement of pseudolines

We (re)introduce Double Permutation Sequences, which provide a combinatorial encoding of arrangements of convex sets in the plane. We also recall the notion of a Topological Affine Plane and several (some new) of its properties. In particular the conjecture of Goodman-Pollack and proved by Habert-Pocchiola, that for every Allowable Double Permutation Sequence there is a universal Topological Affine Plane P (i.e. any finite arrangement of pseudolines is isomorphic to some arrangement of finitely many lines of P), and that every Allowable Double Permutation Sequence can be realized by an arrangement of simply connected sets and pseudoline double tangents to every pair of these sets.

The following applications are then presented:

1 A new proof of the Edelsbrunner-Sharir Theorem: n convex sets in the plane can admit at most 2n-2 geometric permutations and we proved the same via Double Permutation Sequences.

2 The Tverberg (1, k)-separation problem: In 1979 Tverberg asked, what is the smallest number  $f_k$  such that for any family of  $f_k$  mutually disjoint plane convex sets, one set can be separated from k-others and proved that  $f_k$  is finite,

2a In 1980 Hope and Katchalski showed that  $f_k < 12(k-1)$ .

2b In 2010 Mordechai Novick, using double permutation sequences, improved the "Katchalski-Hope" bound to  $f_k < (7.2)(k-1)$ .

Joint work with Raghavan Dhandipani, Jacob E. Goodman, Andreas Holmsen, Shakhar Smorodinsky, Rephael Wenger and Tudor Zamfirescu, supported in part by several NSF grants

Tuesday 2 at 15h15:

## A combinatorial approach to colourful simplicial depth

### Antoine DEZA

(McMaster University, Canada)

The colourful simplicial depth conjecture states that any point in the convex hull of each of d + 1 sets, or colours, of d + 1 points in general position in  $\mathbb{R}^d$  is contained in at least  $d^2 + 1$  simplices with one vertex from each set. We verify the conjecture in dimension 4 and strengthen the known lower bounds in higher dimensions. These results are obtained using a combinatorial generalization of colourful point configurations called octahedral systems. We present properties of octahedral systems generalizing earlier results on colourful point configurations and exhibit an octahedral system which can not arise from a colourful point configuration. The number of octahedral systems is also given.

Joint work with Frédéric Meunier and Pauline Sarrabezolles

Tuesday 2 at 16h30:

## Matroids in tropical geometry

Federico ARDILA

(San Francisco State University, USA)

Each matroid has a polyhedral complex associated to it, called its Bergman complex. These objects play a prominent role in tropical geometry, since they are the tropical analog of linear spaces. I will describe this correspondence and discuss some recent results.

The talk will not assume previous knowledge of tropical geometry.

## Tropical linear spaces and valuated matroids

Felipe RINCON

(University of Warwick, U.K.)

Tropical geometry studies an algebraic variety by 'tropicalizing' it into a combinatorially defined polyhedral complex. Much of the information about the original variety can be recovered from its tropicalization.

In this talk I will show how tropicalized linear spaces are intimately related to valuated matroids and matroid polytopes, and I will explain some of the very nice combinatorics they satisfy. I will also present a similar picture for a more general class of matroids called Coxeter matroids.

Wednesday 3 at 9h:

## Tree decomposition, tree orientation and rigid frameworks

## András RECSKI

(Budapest University of Technology and Economics, Hungary)

One can check in polynomial time if a graph with n vertices and 2n-2 edges can be decomposed into two trees. Similarly, one can check whether a sequence of n non-negative integers adding up to n-1 can be realized as the outdegree-sequence of a properly oriented tree of a given graph with n vertices. Both solutions require the 2-matroid-intersection algorithm. Motivated by a problem in the rigidity of bar-and-joint frameworks we formulate a kind of common generalization of these problems and conjecture that it is still polynomial time solvable.

This work has been supported by the Hungarian Agency for National Development through the research grant TAMOP (contract no. 4.2.2.B-10/1(2010-0009)

Wednesday 3 at 9h45:

# Applying the probabilistic method to Separoids theory

Ricardo STRAUSZ

(UNAM, Mexico)

We will review a couple of applications of the probabilistic method to abstract convexity via the notion of separoids; one related to Tverberg's theorem, and the other to Erdős-Szekeres "happy end" theorem.

Wednesday 3 at 11h:

# The graphicity of the sum of graphic matroids

Csongor CSEHI

(Budapest University of Technology and Economics, Hungary)

There is a conjecture that if the sum of graphic matroids is not graphic then it is nonbinary.

Some special cases have been proved only, for example if several copies of the same graphic matroid are given.

If there are two matroids and the first one can be drawn as a graph with two points, then I formulate an equivalent property for the other matroid for ensuring the graphicity of the sum.

Hence the conjecture holds for this special case.

This work has been supported by the Hungarian Agency for National Development through the research grant TAMOP (contract no. 4.2.2.B-10/1(2010-0009)

#### Wednesday 3 at 11h45:

## Inductive construction and decomposition of graded sparse graphs

Viet Hang NGUYEN

(G-SCOP, Grenoble UJF, France)

Sparse graphs are extensively studied for their role in combinatorial rigidity theory. In this work, we consider graded sparse graphs–a generalization of sparse graphs where different types of edges satisfy different sparsity conditions. We provide an inductive construction and a decomposition into pseudoforests of these graphs. These results generalize the work of Fekete and Szegő on the inductive construction of sparse graphs as well as the work of Streinu and Theran on the decomposition of sparse graphs, thus generalize the original work of Nash-Williams on the decomposition of graphs into forests.

Joint work with Bill Jackson, Queen Mary University, London. Partially supported by the TEO-MATRO grant ANR-10-BLAN 0207

Wednesday 3 at 14h30:

## **Oriented Matroids and Configurations of Points and Lines**

## Jürgen BOKOWSKI

(Technische Universität Darmstadt, Germany)

The theory of oriented matroids can help finding results in the theory of CONFIGURATIONS OF POINTS AND LINES, although in Grünbaum's research monograph from 2009 with this title, he does not stress this aspect very much. The talk reports about applications of oriented matroid techniques that have solved open problems of the theory of configurations of points and lines. *Joint work with Vincent Pilaud* 

Wednesday 3 at 15h15:

## Counting invariants for realizations of associahedra

### Carsten LANGE

(Freie Universität Berlin, Germany)

An n-dimensional associahedron is a simple convex polytope with vertex-edge graph isomorphic to the flip graph of triangulations of a planar convex (n+2)-gon. Generalizing a realization studied by J.-L. Loday, S. Shnider, J. Stasheff and S. Sternberg, a large family of realizations can be easily obtained by choosing a point in the complement of the braid arrangement and a Coxeter element of the corresponding symmetric group. This construction guarantees that the resulting normal fans are coarsenings of the brais arrangement and it can be shown that most of them are linearly nonisomorphic. Hence, the normal cone for each vertex of the associahedron is obtained by merging certain maximal cones of the braid arrangement. For a given Coxeter element, we will discuss the number of vertices of the associahedron where the normal cone consists of exactly k maximal cones of the braid arrangement.

#### Wednesday 3 at 16h30:

# Minimal non-orientable matroids of rank 3

## Hidefumi HIRAISHI

(Graduate school of Information and Technology, University of Tokyo, Japan )

We report on our work on minimal non-orientable matroids of rank 3. There are some well-known minimal non-orientable matroids of rank 3. Among them, the Fano matroid and the MacLane matroid are unique minimal non-orientable matroids of rank 3 with 7 and 8 elements, respectively. Ziegler showed in 1991 that there exists an infinite family of minimal non-orientable matroids of rank 3 with 3n + 2 elements. We construct two new infinite families of minimal non-orientable matroids of rank 3 with 3n and 3n + 1 elements. Our first infinite family with 3n elements starts from one of the two previously known minimal non-orientable matroids of rank 3 with 9 elements, which was discovered in 2012 by Y. Matsumoto et al. Our second infinite family with 3n + 1 elements starts from the Fano matroid. Hence together with Ziegler's infinite family, we now know that there exist minimal non-orientable matroids of rank 3 for every number of elements.

Additionally we examine representability of the two new infinite families, and show in particular that our first infinite family is not representable over any field of characteristic two. *Joint work with Sonoko Moriyama.* 

Wednesday 3 at 17h15:

## **Complete Enumeration of Small Realizable Oriented Matroids**

Hiroyuki MIYATA

(Tohoku University, Japan)

Enumeration of combinatorial types of point configurations and polytopes is a fundamental problem in combinatorial geometry. Although many studies have been done, most of them are for 2-dimensional and non-degenerate cases. Finschi and Fukuda (2002) published the first database of oriented matroids including degenerate (i.e., non-uniform) ones and of higher ranks. After that, large amount of work has been done in order to decide realizability of them.

In this talk, we explain our recent work on algorithmic ways to classify oriented matroids in terms of realizability, which successfully complete the realizability classification of rank 4 oriented matroids with 8 elements, rank 3 oriented matroids with 9 elements and rank 6 oriented matroids with 9 elements. As an application, we determine all possible combinatorial types (including degenerate ones) of 3-dimensional configurations of 8 points, 2-dimensional configurations of 9 points, and 5-dimensional configurations of 9 points. We also determine all possible combinatorial types of 5-polytopes with 9 vertices. In addition, our method is successfully applied to many other problems such as enumeration of PLCP-orientations of the 4-cube (joint work with Komei Fukuda and Lorenz Klaus) recently.

Joint work with Komei Fukuda and Sonoko Moriyama

Thursday 4 at 9h:

## Unbalanced collections, weak maps and a problem in quantum physics

Louis BILLERA

(Cornell University, USA)

We describe the use of a theorem of Dean Lucas on weak maps to give bounds on the number of regions of a hyperplane arrangement arising in thermal field theory and in the theory of threshold functions. While these bounds are not new, the approach seems to be. The real question is whether the number of regions can be computed exactly.

Thursday 4 at 9h45:

# Arrangements of double pseudolines living in non orientable surfaces

## Michel POCCHIOLA

(Institut de Mathématiques de Jussieu, UPMC, Paris)

We show that an arrangement of double pseudolines lives in a sphere with one crosscap if and only if its subarrangements of size 2, 3 and 4 live in spheres with one crosscap.

Thursday 4 at 11h:

## Realization spaces and Erdős-Szekeres theorems for convex sets

#### Andreas HOLMSEN

(KAIST, Republic of Korea)

We consider wiring diagrams where each pair of wires cross at most m times. It turns out that these objects naturally encode what we call the combinatorial-type of an arrangement of compact convex sets in the plane. We will discuss this notion of combinatorial-type and show that it has many nice properties and applications:

- It naturally extends the notion of the order-type of a point configuration in the plane and, more generally, acyclic oriented matroids. In particular every acyclic oriented matroid of rank 3 has a realization by convex sets.

- It unifies various generalizations and conjectures of the classical Erdös-Szekeres theorem. In particular the Erdös-Szekeres constant for families of non-crossing convex sets and for acyclic oriented matroids are the same (which relates a conjecture of Goodman and Pollack to a conjecture of Bisztriczky and Fejes-Toth). Moreover we prove a conjecture of Pach and Tóth extending the previous results to more general arrangements of bodies.

- The realization space of a given order-type is a contractible set, while restricting to configurations of convex k-gons we obtain a generalization of Mnëv's universality theorem. *Joint work with Michael Dobbins and Alfredo Hubard*  Thursday 4 at 11h45:

## From Ehrhart theory to the discrepancy of oriented matroids

### Arnau PADROL

(Universitat Politècnica de Catalunya)

The degree of a point configuration is defined as the maximal codimension of its interior faces. This concept is motivated from a corresponding Ehrhart-theoretic notion for lattice polytopes.

I will present some recent developments concerning point configurations whose degree is small with respect to the dimension of its affine span. These results have several interpretations in areas such as neighborly polytopes or Tverberg theory. *Joint work with Benjamin Nill* 

Friday 5 at 9h:

## The Tutte polynomial as a resultant force

#### Joseph KUNG

(University of North Texas, USA)

Let G be a matrix over a finite field  $\mathbb{K}$  with column set E. A flow G is a row vector in the row space of G, considered as a function on E. A parcel is a subset of the set  $\mathcal{F}$ , defined by  $\mathcal{F} = \{(f,g) : f,g : E \to \mathbb{K}, f - g \text{ is a flow}\}$ . Parcels may be defined by a congruence condition – an equation saying that an algebraical or combinatorial function equals a number modulo a fixed integer n. In this case, n parcels are defined, they partition  $\mathcal{F}$ , and the sum of their sizes, weighted by an appropriate root of unity, is an evaluation of a simple multiple of the Tutte polynomial at a point on a complex hyperbola.

Friday 5 at 9h45:

## Scheduling polynomials

Caroline KLIVANS (Brown University, USA)

We introduce new families of polynomials associated to matroids. Our starting point is the consideration of counting functions which enumerate the number of solutions to certain scheduling problems. These scheduling problems arise naturally in the context of the normal fan of a matroid polytope. From this perspective it is not hard to establish polynomiality of the counting functions. These polynomials do not neccessarily satisfy contraction/deletion and hence are not generally Tutte invariants. For example we define the arboricity polynomial which counts the number of matroid covers with a fixed number of independent sets.

## Matroids over a ring

#### Luca MOCI

(Institut de Mathématiques de Jussieu, Paris 7)

We introduce the notion of a matroid M over a commutative ring R, assigning to every subset of the ground set an R-module according to some axioms. When R is a field, we recover matroids. When R=Z (integers), and when R is a DVR, we get (structures which contain all the data of) quasi-arithmetic matroids, and valuated matroids, respectively. More generally, whenever R is a Dedekind domain, we extend all the usual properties and operations holding for matroids (e.g., duality), and we explicitly describe the structure of the matroids over R. Furthermore, we compute the Tutte-Grothendieck group of matroids over R. By specializing the class of a matroid over Z in the Tutte-Grothendieck group, we obtain the Tutte quasi-polynomial and the arithmetic Tutte polynomial, which have applications to toric arrangements, zonotopes, and graphs. *Joint work with Alex Fink* 

#### Friday 5 at 11h45:

# Local combinatorial formula for the Chern class of combinatorial $S^1$ bundles

#### Nikolai MNEV

(Steklov Mathematical Institute RAS, Russia)

We can identify triangulated oriented  $S^1$ -bundle on a simplicial complex with a decoration of the complex by necklaces.

In terms of such decorations there is a canonical local combinatorial formula for Chern-Euler class and its powers, expressed as a kind of "expectation of parity" of the necklace. The formula can be conceptually attributed to Gelfand - Mac Pherson, M. Kontsevich, M. Kazarjan, A. Gaifullin and others, but it was never published in this simple form. We apply the theory to produce a toy - a triangulated oriented  $S^1$ -bundle canonically associated to a triangulation of oriented surface. The bundle has Chern-Euler number equal to the half of the number of triangles. The triangulated bundles has a property of minimality - they has minimal number of simplexes in the class of all triangulated  $S^1$  - bundles with given Chern number on the oriented surface.

Friday 5 at 14h30:

# Foundations for a theory of phased matroids

Emanuele DELUCCHI

(University of Bremen, Germany)

We introduce "Phased matroids" as a combinatorial abstraction of linear dependency over the complex numbers that parallels the existing theories for general and real linear dependency (given by matroid and oriented matroid theory).

Our theory shares much of the structural richness of oriented matroid theory, yet does not refrain from the occasional "twists and turns" - thereby shedding some new light on known aspects of matroid theory. We have a satisfactory duality theory and several cryptomorphic axiomatizations, including "phirotopes" as introduced by Below, Krummeck and Richter-Gebert. Joint with Laura Anderson

Friday 5 at 15h15:

## Phased Matroids from Gain Graphs

Thomas ZASLAVSKY (Binghamton University (SUNY), USA)

Phased matroids are a complex analog of oriented matroid. Gain graphs are graphs whose edges are invertibly labelled from a group. Gain graphs whose group is that of complex units naturally generate phased matroids which are analogous to graphic matroids. I will report on some aspects of this development.

Joint work with Laura Anderson.

#### Friday 5 at 16h30:

## Realization spaces of phased matroids and the phased matroid Grassmannian

#### Laura ANDERSON

(Binghamton University, SUNY, USA)

Phased matroids are matroids with extra structure. They model vector arrangements over  $\mathbb{C}$  in the same way that oriented matroids model vector arrangements over  $\mathbb{R}$ , and many of the topological questions that arise with oriented matroids are at least as intriguing in the context of phased matroids. I'll discuss some recent unexpected results of my student Amanda Ruiz on realization spaces of phased matroids and some light these results shed on the relationship between complex Grassmannians and the corresponding "phased matroid Grassmannians".

#### Friday 5 at 17h15:

# Discrete Convexity and Polynomial Solvability in Minimum 0-extension Problems

Hiroshi HIRAI

(University of Tokyo)

The minimum 0-extension problem 0-Ext[G] on a graph G is:

given a set V including the vertex set V(G) of G and a nonnegative cost function c defined on the set of all pairs of V, find a 0-extension d of G with  $\langle c, d \rangle$  minimum, where a 0-extension is a metric d on V such that the restriction of d to V(G) coincides with the path metric of G and for all x in V there exists a vertex s in G with d(x,s) = 0. 0-Ext[G] includes a number of basic combinatorial optimization problems, such as minimum (s,t)-cut problem and multiway cut problem.

Karzanov proved the polynomial solvability for a certain large class of modular graphs, and raised the question: What are the graphs G for which 0-Ext[G] can be solved in polynomial time? He also proved that 0-Ext[G] is NP-hard if G is not modular or not orientable (in a certain sense).

In this paper, we prove the converse: if G is orientable and modular, then 0-Ext[G] can be solved in polynomial time. This completes the classification of the tractable graphs for the 0extension problem. To prove our main result, we develop a theory of discrete convex functions on orientable modular graphs, analogous to discrete convex analysis by Murota, and utilize a recent result of Thapper and Zivny on Valued-CSP.

Saturday 6 at 9h:

## Packing of arborescences with matroid constraints

Zoltán SZIGETI

(Ensimag, INP, Grenoble, France)

We provide the directed counterpart of a slight extension of Katoh and Tanigawa's result on rootedtree decompositions with matroid constraints. Our result characterizes digraphs having a packing of arborescences with matroid constraints. It is a proper extension of Edmonds' result on packing of spanning arborescences and implies – using a general orientation result of Frank – the above result of Katoh and Tanigawa.

Joint work with Olivier Durand de Gevigney and Viet Hang Nguyen

Saturday 6 at 9h45:

# A topological characterization of basis graphs of matroids

Jérémie CHALOPIN

(LIF, Université Aix-Marseille, CNRS, France)

The basis graph of a matroid  $\mathcal{M}$  is the graph whose vertices are the bases of  $\mathcal{M}$  and edges are the pairs A, B of bases such that  $|A\Delta B| = 2$ . Basis graphs of matroids have been characterized by Maurer (Matroid basis graphs I, JCTB 14, 1973, 216–240) as graphs satisfying some local conditions and a global metric condition.

In his paper, Maurer conjectured that one can replace his global metric condition by the topological condition of simply connectedness of the triangle-square complex of the graph G (the triangle-square complex of G is a 2-dimensional complex in which the 2-cells are the triangles and the squares of G). We show that the conjecture is true if we strengthen the local conditions.

Joint work with Victor Chepoi (LIF, Aix-Marseille Université) and Damian Osajda (Universtät Wien and Universytet Wrocławski)

Saturday 6 at 11h:

# Shortest Bibranchings and Valuated Matroid Intersection

Kenjiro TAKAZAWA

(RIMS, Kyoto Univ., Japan, and INP, Grenoble, France)

For a digraph D = (V, A) and a partition  $\{S, T\}$  of V, an arc set  $B \subseteq A$  is called an S-T bibranching if each vertex in T is reachable from S and each vertex in S reaches T in the subgraph (V, B). Bibranchings commonly generalize bipartite edge covers and arborescences. A totally dual integral linear system determining the S-T bibranching polytope is provided by Schrijver, and the shortest S-T bibranching problem can be solved in polynomial time by the ellipsoid method or a faster combinatorial algorithm due to Keijsper and Pendavingh.

The valuated matroid intersection problem, introduced by Murota, is a weighted generalization of the independent matching problem. By extending classical combinatorial algorithms for the weighted matroid intersection problem, the valuated matroid intersection problem can be solved with polynomially many value oracles

In this talk, we show that the shortest S-T bibranching problem is polynomially reducible to the valuated matroid intersection problem. This reduction suggests one answer to why the shortest S-T bibranching problem is tractable, and implies new combinatorial algorithms.

## PARTICIPANTS

- **Boris ALBAR** Université Montpellier 2, France
- Laura ANDERSON Binghamton University, SUNY, USA
- Federico ARDILA San Francisco State University, USA
- Hans-Jürgen BANDELT Fachbereich Mathematik, Universität Hamburg
- Louis BILLERA Cornell University, USA
- Jürgen BOKOWSKI Technische Universität Darmstadt, Germany
- Jérémie CHALOPIN LIF, Université Aix-Marseille, CNRS, France
- Jonathan CHAPPELON Université Montpellier 2, France
- Victor CHEPOI Université de la Méditerranée, Aix-Marseille II, France
- Csongor CSEHI Budapest University of Technology and Economics, Hungary
- Anna DE MIER Universitat Politècnica de Catalunya
- **Emanuele DELUCCHI** University of Bremen, Germany
- Antoine DEZA McMaster University, Canada
- Martin DLUGOSCH University of Bremen, Germany
- **Olivier DURAND DE GEVIGNEY** INP, Grenoble, France
- **Eva Maria FEICHTNER** University of Bremen, Germany
- David FORGE Université Paris-Sud Orsay, France
- Komei FUKUDA ETH Zurich, Switzerland
- **Emeric GIOAN** CNRS, LIRMM, Université Montpellier 2, France
- Antonio GONZALEZ I3M, Université Montpellier 2, France
- António GUEDES DE OLIVEIRA University of Porto, Portugal
- Guillaume GUEGAN LIRMM, Université Montpellier 2, France
- Hiroshi HIRAI University of Tokyo
- Hidefumi HIRAISHI Graduate school of Information and Technology, University of Tokyo, Japan
- Andreas HOLMSEN KAIST, Republic of Korea
- Caroline KLIVANS Brown University, USA

Kolja KNAUER Technische Universität Berlin, Germany Matjaž KOVŠE University of Leipzig, Germany Geza KULCSAR Budapest University of Technology and Economics, Hungary Joseph KUNG University of North Texas, USA Carsten LANGE Freie Universität Berlin, Germany **Bodo LASS** Université Lyon 1, France Jim LAWRENCE George Mason University, USA Goran MALIC University of Manchester **Glenn MERLET** Institut de Mathématiques de Luminy, France Cynthia MERRICK George Mason University, USA Hiroyuki MIYATA Tohoku University, Japan Nikolai MNEV Steklov Mathematical Institute RAS, Russia Luca MOCI Institut de Mathématiques de Jussieu, Paris 7 Luis MONTEJANO Université Montpellier 2, France Sonoko MORIYAMA Graduate School of Information Sciences, Tohoku University Viet Hang NGUYEN G-SCOP, Grenoble UJF, France Damian OSAJDA Universitaet Wien Austria et Uniwersytet Wroclawski, Poland Arnau PADROL Universitat Politècnica de Catalunya Vincent PILAUD Ecole Polytechnique, France Michel POCCHIOLA Institut de Mathématiques de Jussieu, UPMC, Paris **Richard POLLACK** New York University, USA Myriam PREISSMANN G-SCOP, INP, Grenoble, France Jorge RAMIREZ ALFONSIN Université Montpellier 2, France András RECSKI Budapest University of Technology and Economics, Hungary Felipe RINCON University of Warwick, U.K. Jean-Pierre ROUDNEFF Lycée Louis-le-Grand, Paris 6ème Kevin SOL Université Montpellier 2, France Daria STEPANOVA Université Montpellier 2, France

Ricardo STRAUSZ	UNAM, Mexico
Zoltán SZIGETI	Ensimag, INP, Grenoble, France
Kenjiro TAKAZAWA	RIMS, Kyoto Univ., Japan, and INP, Grenoble, France
Véronique VENTOS	Université Paris-Sud Orsay, France
Thomas ZASLAVSKY	Binghamton University (SUNY), USA

