

ONTOLOGY-MEDIATED QUERY ANSWERING

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ONTOLOGY-MEDIATED QUERY ANSWERING (OMQA)



**incomplete
database**
(ground facts)

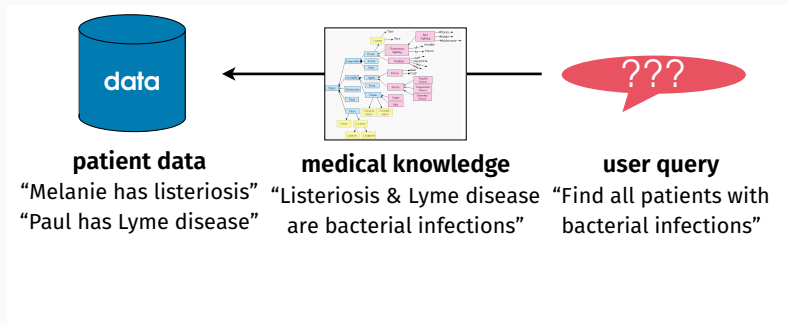


ontology
(logical theory)



user query

ONTOLOGY-MEDIATED QUERY ANSWERING (OMQA)



The **ontology** (logical theory) specifies:

- **terminology** (or vocabulary) of the domain
- **semantic relationships** between terms
 - relations of specificity or generality, equivalence, disjointness, ...

ONTOLOGY-MEDIATED QUERY ANSWERING (OMQA)



patient data

“Melanie has listeriosis”
“Paul has Lyme disease”



medical knowledge

“Listeriosis & Lyme disease
are bacterial infections”



user query

“Find all patients with
bacterial infections”

expected answers: Melanie, Paul

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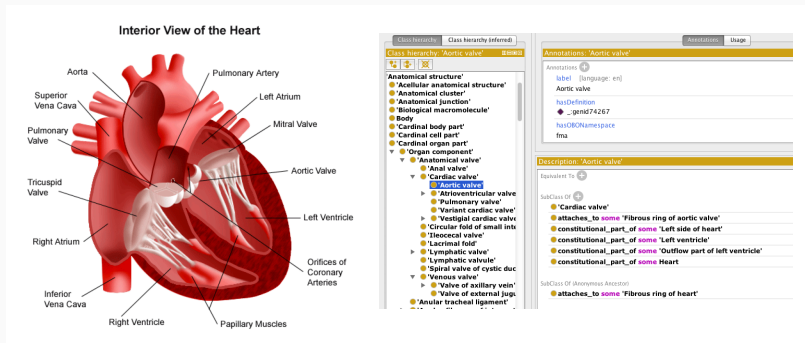
- ontology can be used to **enrich the data vocabulary**, making it **easier for users to formulate their queries**
- especially useful when **integrating multiple data sources**

To support **automated reasoning**

- **uncover implicit connections** between terms, **errors in modelling**
- **exploit knowledge in the ontology during query answering**, to get back a **more complete set of answers** to queries

APPLICATIONS OF OMQA: MEDICINE

General medical ontologies: **SNOMED CT** (~ 400,000 terms!), GALEN
Specialized ontologies: FMA (anatomy), NCI (cancer), ...

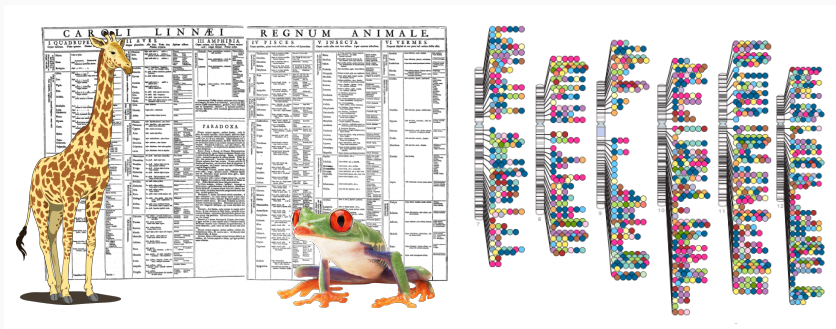


Querying & exchanging medical records (find patients for medical trials)

· myocardial infarction vs. MI vs. heart attack vs. 410.0

Supports tools for **annotating and visualizing patient data** (scans, x-rays)

Hundreds of ontologies at BioPortal (<http://bioportal.bioontology.org/>):
Gene Ontology (GO), Cell Ontology, Pathway Ontology, Plant Anatomy, ...

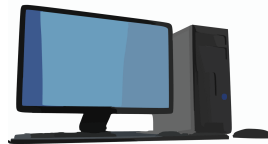


Help scientists **share, query, & visualize** experimental data

APPLICATIONS OF OMQA: ENTREPRISE INFORMATION SYSTEMS

Companies and organizations have **lots of data**

- **need easy and flexible access** to **support decision-making**



Example industrial projects:

- **Public debt data:** Sapienza Univ. & Italian Department of Treasury
- **Energy sector:** Optique EU project (several univ, StatOil, Siemens)

Ontologies typically described using **logic-based formalisms**

Description logics (DLs)

- family of **decidable fragments of first-order logic (FO)**
- concise **variable-free syntax**
- only **unary and binary predicates**

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- family of languages of rules of the form $\forall \vec{x} (\exists \vec{y} \varphi(\vec{x}, \vec{y}) \rightarrow \exists \vec{z} \psi(\vec{x}, \vec{z}))$
where $\varphi(\vec{x}, \vec{y})$ and $\psi(\vec{x}, \vec{z})$ are conjunctions of atoms
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Two approaches are **incomparable and complementary**

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Computational properties well understood (decidability, complexity)

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Computational properties well understood (decidability, complexity)

Many implemented reasoners and tools available for use

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- forward chaining (chase) halts
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- tree-like models

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Many complexity & decidability results, **few implemented algorithms**

Can consider **extensions allowing equality, disjunction in rule heads**

- such extensions less well understood

Introduction to DLs

Introduction to OMQA

Techniques for OMQA with Lightweight DLs

Research Questions in OMQA

INTRODUCTION TO DLS

Building blocks:

- **concept names** (unary predicates, classes)
- **role names** (binary predicates, properties)
- **individual names** (constants)

Prof Fellow Course

teaches headOf

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Constructors to build complex concepts and roles $\sqcup, \sqcap, \neg, \forall, \exists, \dots$

$\text{Faculty} \sqcap \neg \text{Prof}$

$\exists \text{teaches. GradCourse}$

teaches^-

Note: allowed constructors **depends on chosen DL**

DL knowledge base (KB) = **ABox** (data) + **TBox** (ontology)

ABox = finite set of **concept and role assertions (facts)**

Prof(anna)

teaches(tom, cs101)

TBox (ontology) = finite set of **axioms**

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TBox (ontology) = finite set of **axioms**

- **concept inclusions** $C \sqsubseteq D$ (C, D possibly complex concepts)

Prof \sqsubseteq Faculty

$\exists \text{teaches.GradCourse} \sqsubseteq \text{Prof}$

- **role inclusions** $R \sqsubseteq S$ (R, S possibly complex roles)

taughtBy \sqsubseteq teaches⁻

headOf \sqsubseteq memberOf

Note: allowed axioms **depends on chosen DL**

Professors and lecturers are disjoint classes of faculty

$$\text{Prof} \sqsubseteq \text{Faculty} \quad \text{Lect} \sqsubseteq \text{Faculty} \quad \text{Prof} \sqsubseteq \neg \text{Lect}$$

Every course is either an undergrad or grad course

$$\text{Course} \sqsubseteq \text{UCourse} \sqcup \text{GCourse}$$

The relation takesCourse connects students to courses

$$\exists \text{takesCourse}.T \sqsubseteq \text{Student} \quad \exists \text{takesCourse}^{-}.T \sqsubseteq \text{Course}$$

Every student takes at least 2 and at most 5 courses

$$\text{Student} \sqsubseteq \geq 2 \text{takesCourse}.T \sqcap \leq 5 \text{takesCourse}.T$$

Every **grad student** is **supervised by some faculty member**

$$\text{GStudent} \sqsubseteq \exists \text{supervisedBy.Faculty}$$

The **academic ancestor** relation is **transitive**

$$\text{supervisedBy} \sqsubseteq \text{academicAnc} \quad \text{trans}(\text{academicAnc})$$

Students who **only take grad-level courses** are **grad students**

$$\text{Student} \sqcap \forall \text{takesCourse.GCourse} \sqsubseteq \text{GStudent}$$

FO translation:

$$\forall x (\text{Student}(x) \wedge (\forall y \text{ takesCourse}(x, y) \rightarrow \text{GCourse}(y)) \rightarrow \text{GStudent}(x))$$

Interpretation \mathcal{I} (“possible world”)

(like in first-order logic)

- **domain of objects** $\Delta^{\mathcal{I}}$ (possibly infinite set)
- **interpretation function** $\cdot^{\mathcal{I}}$ that maps
 - **concept name** $A \rightsquigarrow$ set of objects $A^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}}$
 - **role name** $r \rightsquigarrow$ set of pairs of objects $r^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}}$
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Interpretation function $\cdot^{\mathcal{I}}$ extends to **complex concepts and roles**:

\top	$\Delta^{\mathcal{I}}$
\perp	\emptyset
$\neg C$	$\Delta^{\mathcal{I}} \setminus C^{\mathcal{I}}$
$C_1 \sqcap C_2$	$C_1^{\mathcal{I}} \cap C_2^{\mathcal{I}}$
$\exists R.C$	$\{d_1 \mid \text{there exists } (d_1, d_2) \in R^{\mathcal{I}} \text{ with } d_2 \in C^{\mathcal{I}}\}$
$\forall R.C$	$\{d_1 \mid d_2 \in C^{\mathcal{I}} \text{ for all } (d_1, d_2) \in R^{\mathcal{I}}\}$
r^-	$\{(d_2, d_1) \mid (d_1, d_2) \in r^{\mathcal{I}}\}$

Satisfaction in an interpretation

- \mathcal{I} satisfies $C \sqsubseteq D \iff C^{\mathcal{I}} \subseteq D^{\mathcal{I}}$
- \mathcal{I} satisfies $R \sqsubseteq S \iff R^{\mathcal{I}} \subseteq S^{\mathcal{I}}$
- \mathcal{I} satisfies $A(a) \iff a^{\mathcal{I}} \in A^{\mathcal{I}}$
- \mathcal{I} satisfies $r(a, b) \iff (a^{\mathcal{I}}, b^{\mathcal{I}}) \in r^{\mathcal{I}}$

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Model of a KB \mathcal{K} = interpretation that satisfies all statements in \mathcal{K}

\mathcal{K} is satisfiable = \mathcal{K} has at least one model

\mathcal{K} entails α (written $\mathcal{K} \models \alpha$) = every model \mathcal{I} of \mathcal{K} satisfies α

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Basic reasoning tasks:

- **KB satisfiability**: decide whether \mathcal{K} is satisfiable
- **Axiom entailment**: decide whether $\mathcal{T} \models \alpha$ (with α an axiom)
 - **Classification**: decide $\mathcal{T} \models A \sqsubseteq B$ for every pair A, B of concept names

ABoxes are interpreted under the **open-world assumption**

- **facts that are not in the ABox may still be true** (e.g. can be inferred by exploiting information in the TBox)
- **differs** from the **typical closed-world assumption** from databases, where **absent facts are interpreted as false**

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Semantics in terms of **arbitrary (possibly infinite) interpretations**

- **differs from finite models** considered in **databases**
- may consider an **alternative semantics based upon finite models**
 - for some DLs, two semantics behave the same
 - for others, often possible to reduce to arbitrary model reasoning

For today's talk, we'll focus on standard semantics (arbitrary models)

Prototypical expressive description logic *ALC*:

- Concepts: $C := \top \mid \perp \mid A \mid \neg C \mid C \sqcap C \mid C \sqcup C \mid \exists r.C \mid \forall r.C$
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Highly expressive description logic \mathcal{SHOIQ}

(~ OWL 2)

- Extends \mathcal{ALC} with:
 - **number restrictions** $\leq nR.C$ $\geq nR.C$ and **nominals** $\{a\}$
 - **role inclusions** $R_1 \sqsubseteq R_2$ and transitivity axioms $trans(R)$
 - **inverse roles** r^- (allowed in all types of axioms)

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\mathcal{ALCI} = extension of \mathcal{ALC} with **inverse roles** (\mathcal{I})

\mathcal{ELH} = extension of \mathcal{EL} with **role inclusions** (\mathcal{H})

INTRODUCTION TO OMQA

Instance queries (IQs): find instances of a given concept or role

Faculty(x)

teaches(x, y)

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conjunctions of atoms, some variables can be existentially quantified

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(find all faculty members that teach something)

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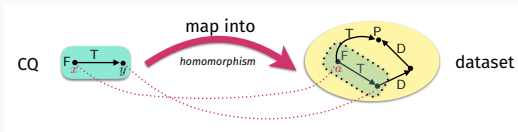
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Ontology-mediated query (OMQ):

pair (\mathcal{T}, q) with \mathcal{T} a TBox and q a query (IQ / CQ)

QUERY ANSWERING: DATABASE VS ONTOLOGY SETTINGS

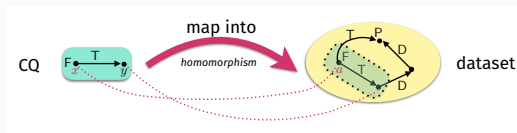
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database D + query $q \rightsquigarrow$ set of answers $ans(q, D)$

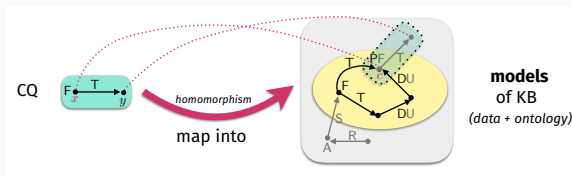
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Answering CQs in the **presence of a TBox (ontology)**



model \mathcal{I} of KB $(\mathcal{T}, \mathcal{A})$ + query $q \rightsquigarrow$ set of answers $ans(q, \mathcal{I})$

Question: how to combine the answers from different models?

Certain answers:

- tuples of inds \vec{a} such that $\vec{a} \in \text{ans}(q, \mathcal{I})$ for every model \mathcal{I} of $(\mathcal{T}, \mathcal{A})$
- corresponds to a form of entailment, we'll write $\mathcal{T}, \mathcal{A} \models q(\vec{a})$

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Ontology-mediated query answering =

problem of computing / verifying **certain answers**

TBox (ontology):

$$\begin{aligned} \text{Prof} &\sqsubseteq \text{Faculty} & \text{Fellow} &\sqsubseteq \text{Faculty} & \text{Prof} &\sqsubseteq \neg \text{Fellow} \\ \text{Prof} &\sqsubseteq \exists \text{teaches}.\top & \exists \text{teaches}^{\neg}.\top &\sqsubseteq \text{Course} \end{aligned}$$

ABox (data):

$$\{\text{Prof}(\text{anna}), \text{Fellow}(\text{tom}), \text{teaches}(\text{tom}, \text{cs101})\}$$

Query: $q(x) = \exists y. \text{Faculty}(x) \wedge \text{teaches}(x, y)$

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Get the following certain answers:

- anna $\text{Prof}(\text{anna}) + \text{Prof} \sqsubseteq \text{Faculty} + \text{Prof} \sqsubseteq \exists \text{teaches}.\text{T}$
- tom $\text{Fellow}(\text{tom}) + \text{Fellow} \sqsubseteq \text{Faculty} + \text{teaches}(\text{tom}, \text{cs101})$

OMQA viewed as a **decision problem** (yes-or-no question):

PROBLEM: **\mathcal{Q} answering in \mathcal{L}** (\mathcal{Q} a query language, \mathcal{L} a DL)

INPUT: An n -ary query $q \in \mathcal{Q}$, an **ABox** \mathcal{A} , an **\mathcal{L} -TBox** \mathcal{T} ,
and a **tuple** $\vec{a} \in \text{Ind}(\mathcal{A})^n$

QUESTION: **Does $\mathcal{T}, \mathcal{A} \models q(\vec{a})$?**

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Combined complexity: in terms of **size of whole input**

Data complexity: in terms of **size of \mathcal{A} only**

- **view rest of input as fixed** (of constant size)
- **motivation:** ABox (data) typically much larger than rest of input

data complexity \leq **combined complexity**

Recall the DL \mathcal{ALC} : $C := \top \mid \perp \mid A \mid \neg C \mid C \sqcap C \mid C \sqcup C \mid \exists r.C \mid \forall r.C$

Satisfiability, IQ answering, and CQ answering in \mathcal{ALC} are:

- EXPTIME-complete in combined complexity
- coNP-complete in data complexity

Even worse news for CQ answering in \mathcal{ALCI} ($= \mathcal{ALC}$ + inverse roles):

- 2EXPTIME-complete in combined complexity
- coNP-complete in data complexity

OMQA WITH LIGHTWEIGHT DLS

Negative results led to proposal of **new DLs with lower complexity**

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DL-Lite family of DLs

(basis for **OWL 2 QL**)

- designed with OMQA in mind
- capture main constructs from **conceptual modelling**
- key technique: **query rewriting** (~ backward chaining)

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- well suited for **medical and life science applications**
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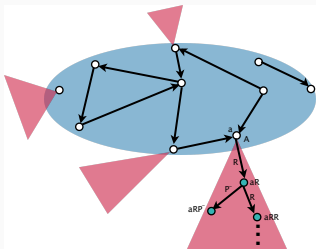
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Commonality: **cannot express disjunction (Horn logics)**,
existence of a **canonical / universal model**

CANONICAL MODELS

For **Horn ontologies** (no form of disjunction) like DL-Lite, \mathcal{EL} :
enough to consider a single **canonical model**

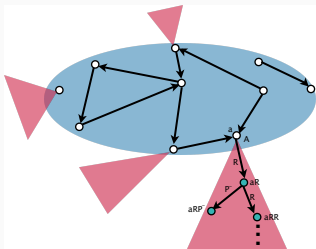
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CANONICAL MODELS

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OMQA with Horn DLs =
finding ways to
map the query into
the **canonical model**

We present the **dialect DL-Lite_R** (which underlies **OWL2 QL profile**).

DL-Lite_R TBoxes contain

- **concept inclusions** $B_1 \sqsubseteq B_2, B_1 \sqsubseteq \neg B_2$
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where $B := A \mid \exists R$ $R := r \mid r^-$

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Example TBox inclusions:

- Every professor teaches something: **Prof** $\sqsubseteq \exists \text{teaches}$
- Everything that is taught is a course: $\exists \text{teaches}^- \sqsubseteq \text{Course}$
- Head of dept implies member of dept: **headOf** $\sqsubseteq \text{memberOf}$

Idea: reduce OMQA to database query evaluation

- **rewriting step**: TBox \mathcal{T} + query $q \rightsquigarrow$ first-order (SQL) query q'
- **evaluation step**: evaluate query q' using relational DB system

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Good news: **every CQ and DL-Lite ontology has FO-rewriting**

EXAMPLE: QUERY REWRITING IN DL-LITE

Reconsider the DL-Lite TBox \mathcal{T} :

$\text{Prof} \sqsubseteq \text{Faculty}$ $\text{Fellow} \sqsubseteq \text{Faculty}$ $\text{Prof} \sqsubseteq \neg \text{Fellow}$
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Evaluating the rewritten query over the earlier ABox

$\{\text{Prof}(\text{anna}), \text{Fellow}(\text{tom}), \text{teaches}(\text{tom}, \text{cs101})\}$

produces the two certain answers: anna and tom

Can focus w.l.o.g. on **rewritings over consistent ABoxes**

“Classic” approach works roughly as follows on input (q, \mathcal{T}) :

- Start with $S = \{q\}$
- **Until S stabilizes, pick some $q' \in S$ and do one of the following:**
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Alternative “semantic” approach (also producing a UCQ):

- Big \bigvee over possible decompositions of q into ABox and “tree parts”
- For atoms mapped to ABox: check if **find implying atom in data**
- For **subqueries mapped to tree parts**:
 - ensure **generating atom in data, merge “root” variables**

Data complexity:

- rewriting takes **constant time**, yields FO query
- upper bound from FO query evaluation: **AC_0** ($AC_0 \subseteq \text{LOGSPACE} \subseteq P$)
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Combined complexity:

- ‘guess’ a disjunct of UCQ-rewriting and how to map it into ABox
- **CQ answering** is **NP-complete** (same as for DBs)
- **IQ answering** is **NLOGSPACE-complete** ($NLOGSPACE \subseteq P$)

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- Rewriting: $\bigvee_{(i_1, \dots, i_n) \in \{0,1\}^n} A_1^{i_1}(x) \wedge A_2^{i_2}(x) \wedge \dots \wedge A_n^{i_n}(x)$

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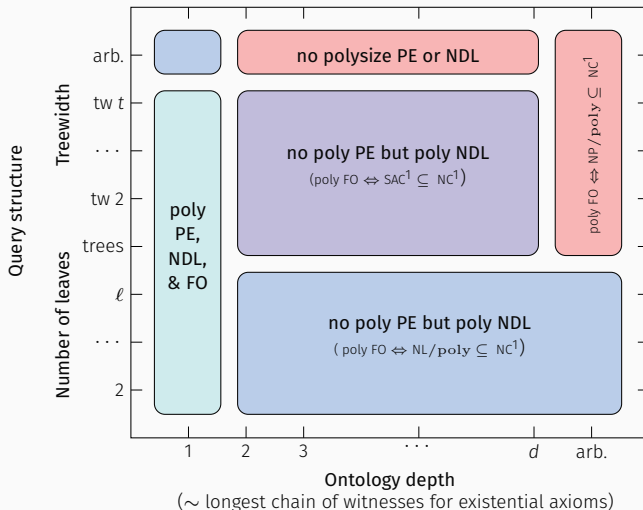
What happens if we adopt other representations?

- **positive existential queries (PE)**, **non-recursive Datalog (NDL)**,
first-order queries (FO)

SUCCINCTNESS LANDSCAPE FOR DL-LITE

(for DL-Lite_R ontologies, so-called 'pure' rewritings)

no poly PE but poly NDL
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Next consider the logic \mathcal{EL} :

- Concepts: $C := \top \mid A \mid C \sqcap C \mid \exists r.C$
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We start with IQs and present a **saturation-based approach**.

Convenient to assume \mathcal{EL} TBoxes given in **normal form**:

$$A_1 \sqcap \dots \sqcap A_n \sqsubseteq B \quad A \sqsubseteq \exists r.B \quad \exists r.A \sqsubseteq B$$

(A, A_i, B concept names or \top)

TBox rules

$$\frac{A \sqsubseteq B_i \ (1 \leq i \leq n) \quad B_1 \sqcap \dots \sqcap B_n \sqsubseteq D}{A \sqsubseteq D} \text{ T1} \qquad \frac{A \sqsubseteq B \quad B \sqsubseteq \exists r.D}{A \sqsubseteq \exists r.D} \text{ T2}$$

$$\frac{A \sqsubseteq \exists r.B \quad B \sqsubseteq D \quad \exists r.D \sqsubseteq E}{A \sqsubseteq E} \text{ T3}$$

ABox rules

$$\frac{A_1 \sqcap \dots \sqcap A_n \sqsubseteq B \quad A_i(a) \ (1 \leq i \leq n)}{B(a)} \text{ A1} \qquad \frac{\exists r.B \sqsubseteq A \quad r(a, b) \quad B(b)}{A(a)} \text{ A2}$$

Algorithm: **apply rules exhaustively**, check if $A(a) \ (r(a, b))$ is present

EXAMPLE: SATURATION IN EL

PenneArrabiata $\sqsubseteq \exists \text{hasIngred}.\text{ArrabiataSauce}$ (1)

PenneArrabiata $\sqsubseteq \text{PastaDish}$ (2)

PastaDish $\sqsubseteq \text{Dish}$ (3)

PastaDish $\sqsubseteq \exists \text{hasIngred}.\text{Pasta}$ (4)

ArrabiataSauce $\sqsubseteq \exists \text{hasIngred}.\text{Peperoncino}$ (5)

Peperoncino $\sqsubseteq \text{Spicy}$ (6)

$\exists \text{hasIngred}.\text{Spicy} \sqsubseteq \text{Spicy}$ (7)

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ArrabSauce $\sqsubseteq \text{Spicy}$	T3 : (5), (6), (7)	(10)
PenneArrab $\sqsubseteq \text{Spicy}$	T3 : (1), (10), (7)	(11)
PenneArrab $\sqsubseteq \text{Dish}$	T1 : (2), (3)	(12)
PenneArrab $\sqsubseteq \exists \text{hasIngred. Pasta}$	T2 : (2), (4)	(13)
PenneArrab $\sqsubseteq \text{SpicyDish}$	T1 : (11), (12), (8)	(14)
Spicy(<i>p</i>)	A1 : (11), (9)	(15)
Dish(<i>p</i>)	A1 : (12), (9)	(16)
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Procedure runs in **polynomial time** in $|\mathcal{K}|$. This is **optimal**:

IQ answering in \mathcal{EL} is **P-complete for data & combined complexity**

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- rules that **generate** all entailed facts over original individuals
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P data complexity extends to much **richer Horn DLs**

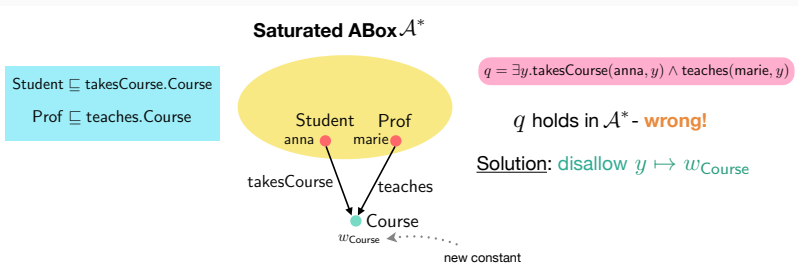
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- saturate ABox using TBox axioms
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COMBINED APPROACH TO CQ ANSWERING IN EL

Way to use relational DBs to do CQ answering in \mathcal{EL} :

- **saturate ABox** using TBox axioms
 - introduce new individuals to witness existentials on LHS ($A \sqsubseteq \exists r.B$)
 - to ensure finite: reuse individuals as witnesses
 - can be viewed as compact representation of canonical model
- **evaluate** query on saturated ABox \Rightarrow **superset of certain answers**
- two strategies to **block unsound answers**:
 - add extra conditions to query
 - post-processing to identify and remove false answers



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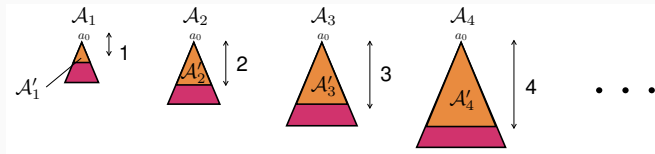
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FO-rewritability is EXPTIME-complete in $(\mathcal{EL}, \text{IQ})$ and $(\mathcal{EL}, \text{CQ})$

Characterization of non-existence of FO-rewriting

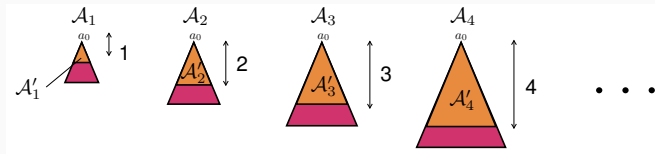
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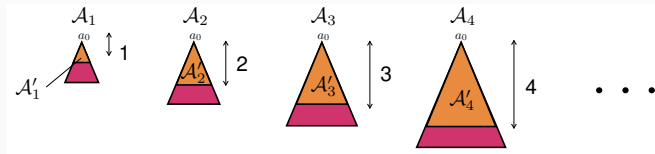
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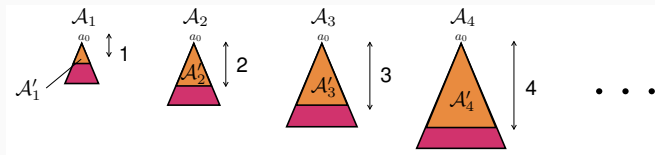
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Can **generalize this technique** to handle CQs and richer Horn DLs

LINKING TO EXISTING DATA VIA MAPPINGS

So far: data given as ABox (unary + binary facts using TBox predicates)

Problem: how to apply the approach to **existing relational data** (arbitrary arity, different vocabulary)?

Solution: use **mapping** that specifies **relationship** between the **database relations** and the **ontology predicates**

Formally: **mapping assertions** of the form $\forall \vec{x} \varphi(\vec{x}) \rightarrow \psi(\vec{x})$ where:

- $\varphi(\vec{x})$ is a query formulated using DB relations
- $\psi(\vec{x})$ is a query in the ontology vocabulary

Global-as-view (GAV) mappings: **ψ is an atom** (without \exists -vars)

Database D + mapping $\mathcal{M} \rightsquigarrow$ **ABox** $\mathcal{A}_{\mathcal{M},D}$

Models of $\langle \mathcal{T}, \mathcal{M}, D \rangle$ = models of the KB $\langle \mathcal{T}, \mathcal{A}_{\mathcal{M},D} \rangle$

Certain answers to q w.r.t. $\langle \mathcal{T}, \mathcal{M}, D \rangle$ =
 tuples of **constants a from $D \cup \mathcal{M}$** such that $\langle \mathcal{T}, \mathcal{A}_{\mathcal{M},D} \rangle \models q(a)$

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Handling mappings:

- apply mappings to **generate ABox, proceed as usual**
- **virtual ABox**: combine query rewriting with an extra **unfolding step** to get **rewriting over DB relations**

EXAMPLE: MAPPINGS

Suppose course data is stored in the two database tables:

UndergradCourses[CourseID, Year, Lecturer, Room, Timeslot]

GradCourses[CourseID, Lecturer, Room, Timeslot]

and employee data is stored in the table

Employee[EmpID, Name, Position, Dept]

The mapping could contain statements like: (initial \forall omitted)

$\exists y, r, t$ **UndergradCourses**(c, y, l, r, t) \rightarrow **teaches**(l, c)

$\exists y, r, t$ **GradCourses**(c, l, r, t) \rightarrow **teaches**(l, c)

$\exists n, d$ **Employee**(x, n, Professor, d) \rightarrow **Prof**(x)

to populate the ontology predicates **teaches** and **Prof**

Unfolding of query q (over ontology vocabulary) w.r.t. mapping:

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For $q(x, y) = \text{Prof}(x) \wedge \text{teaches}(x, y)$, unfolding yields the following:

$$\begin{aligned} & \exists n, d, z, r, t \text{Employee}(x, n, \text{Professor}, d) \wedge \text{UndergradCourses}(y, z, x, r, t) \\ \vee & \exists n, d, r, t \text{Employee}(x, n, \text{Professor}, d) \wedge \text{GradCourses}(y, x, r, t) \end{aligned}$$

Observe **result uses only DB predicates**, can be converted to SQL

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- replace atoms in q by the bodies of (unified) matching rules

For $q(x, y) = \text{Prof}(x) \wedge \text{teaches}(x, y)$, unfolding yields the following:

$$\begin{aligned} & \exists n, d, z, r, t \text{Employee}(x, n, \text{Professor}, d) \wedge \text{UndergradCourses}(y, z, x, r, t) \\ \vee & \exists n, d, r, t \text{Employee}(x, n, \text{Professor}, d) \wedge \text{GradCourses}(y, x, r, t) \end{aligned}$$

Observe **result uses only DB predicates**, can be converted to SQL

Opportunities for optimization: simplify rewriting by exploiting the fact that only needs to work for **ABoxes induced by the mapping**

OMQA RESEARCH

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Support for **building and maintaining** OMQA systems

- ontology + mapping **bootstrapping**, **module extraction**, **debugging**, ontology **evolution** and **versioning**
- inspired **new reasoning tasks**: query inseparability, query emptiness, justification finding, logical difference, ...

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Beyond classical OMQA:

- **inconsistency-tolerant** query answering
- **probabilistic** query answering
- **privacy-aware** query answering

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