# Tracing the Dark Matter Web

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### Outline of the talk

- Brief cosmological introduction
- Beginning of the dark matter web story
  - The Zeldovich approximation
  - Geometrical and topological challenges
  - Web of galaxies
- Dark matter web
  - Flip-flop field as a record of halo merging
  - Multi stream field
  - A comparison project "Tracing the Cosmic Web"
  - Caustics
- Summary

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## Structure in the Universe

*Universe, 380,000 year old Gaussian random Field* 



## Plank map

Temperature fluctuations of Cosmic Microwave Background T=2.73 K (fluctuations: of the order of 1/100,000)

### At present (13.7 billion year old) Highly non-Gaussian

Below is the image in its original context on the page: www.astro.princeton.edu/ ~mjuric/universe/



Galaxy distribution in a thin slice

# Why did inhomogeneities grow? - Thanks to gravitational instability of Dark Matter Why only Dark matter? more mass - stronger gravity

Dark Matter 26.8%

Neutrinos

10%

Photons

Atoms 12%

15%

TODAY

13.7 BILLION YEARS AGO (Universe 380,000 years old) Dark

Matter

63%

Atoms alone could NOT develop structures because they were unable to overcome the expansion of the universe!





## **Cosmological parameters (Plank 2015)**

Calcu- lated values	Hubble constant	0.7%	H <sub>0</sub>	$67.74 \pm 0.46 \text{ km s}^{-1} \text{ Mpc}^{-1}$
	Baryon density parameter <sup>[b]</sup>	2%	Ω <sub>b</sub>	0.0486 ±0.0010 <sup>[e]</sup>
	Dark matter density parameter <sup>[b]</sup>	2.2%	Ω <sub>c</sub>	0.2589 ±0.0057 <sup>[f]</sup>
	Matter density parameter <sup>[b]</sup>	2%	Ω <sub>m</sub>	0.3089 ±0.0062
	Dark energy density parameter <sup>[b]</sup>	0.9%	Ω <sub>Λ</sub>	0.6911 ±0.0062
	Critical density	1.4%	ρ <sub>crit</sub>	$(8.62 \pm 0.12) \times 10^{-27} \text{ kg/m}^{3[g]}$
	Fluctuation amplitude at 8h <sup>-1</sup> Mpc	1%	$\sigma_8$	0.8159 ±0.0086
	Redshift at decoupling		Ζ.	1 089.90 ±0.23
	Age at decoupling		t.	377 700 ±3200 years <sup>[16]</sup>
	Redshift of reionization (with uniform	<b>z</b> <sub>re</sub>	8.5 <sup>+1.0</sup> <sub>-1.1</sub> <sup>[17]</sup>	

### Linear growth of density inhomogeneities:

- linearized equations => analytic solution
- amplitude grows but shapes do not change (Gaussian)
- density contrast: (den <den>)/<den> << 1</li>

### **Nonlinear evolution**

- non-linear equations => approximations and numerical
- both geometry and topology evolve dramatically (non G)
- density contrast: (den <den>)/<den> >> 1

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### Gravitational Instability

Usually the growth of density perturbations is described in the comoving coordiantes

$${f x}\equiv rac{1}{a(t)}{f r}$$

and in terms of peculiar velocity

$$\mathbf{v}_p \equiv \mathbf{v} - H(t)\mathbf{r},$$

where a(t) is the scale factor describing the uniform expansion of the universe and  $H(t) \equiv \dot{a}/a$  is the Hubble parameter.

$$\Omega = 1; \quad a(t) \propto t^{2/3}$$

### **Rescaling Variables**

$$\eta \equiv a^{3}
ho$$
  
 $\mathbf{v} \equiv (a\dot{D})^{-1}\mathbf{v}_{p} = \dot{D}^{-1}rac{d\mathbf{x}}{dt} = rac{d\mathbf{x}}{dD}$   
 $arphi \equiv \left(rac{3}{2}\Omega_{0}\dot{a}^{2}D
ight)^{-1}\phi$ 

Significantly simplifies the equations

(1) continuity or conservation of mass (2) Euler equation, (3) Poisson  $\begin{aligned}
\frac{\partial \eta}{\partial D} + \nabla_x \cdot (\eta \mathbf{v}) &= 0, \\
\frac{\partial \mathbf{v}}{\partial D} + (\mathbf{v} \cdot \nabla_x) \mathbf{v} &= -\frac{3}{2} \frac{\Omega_0}{D f_z^2} (\nabla_x \varphi + \mathbf{v}), \\
\frac{\partial \mathbf{v}}{\partial D} + (\mathbf{v} \cdot \nabla_x) \mathbf{v} &= -\frac{3}{2} \frac{\Omega_0}{D f_z^2} (\nabla_x \varphi + \mathbf{v}), \\
\nabla_x^2 \varphi &= \frac{\delta}{D}
\end{aligned}$ 

where D = D(t) is a monotonically growing function of time,  $\Omega_0 \approx 0.27$  is the dimensionless mean density of matter in the universe at present,  $f(t) = d \ln D/d \ln a$ , and  $\delta = (\eta - \bar{\eta})/\bar{\eta} = (\rho - \bar{\rho})/\bar{\rho}$ .

$$\Omega = 1; \quad D(t) = a(t); \quad f = 1$$

12/04/2009

11

Astron. & Astrophys. 5, 84-89 (1970)

#### Gravitational Instability: An Approximate Theory for Large Density Perturbations

YA. B. ZELDOVICH Institute of Applied Mathematics, Moscow

Received September 19, 1969

## Zel'dovich approximation (1970)

Comoving coordinates:  $X_i$ ,

Zel'dovich approximation is a map:  $\mathbf{x}_i(\mathbf{q}, t) = q_i + D(t)s_i(\mathbf{q})$ 

If  $\Phi(\mathbf{q})$  is the linear perturbation of grav. potential then  $s_i(\mathbf{q}) = -\partial \Phi / \partial q_i$ 

Density can be found from the conservation of mass

$$\rho(\mathbf{q},t) = \bar{\rho}(t) \left| \frac{\partial r_i}{\partial q_k} \right|^{-1} = \bar{\rho} \left| \left[ (1 - D(t)\alpha(\mathbf{q}))^{-1} \left[ (1 - D(t)\beta(\mathbf{q}))^{-1} \left[ (1 - D(t)\gamma(\mathbf{q}))^{-1} \right] \right]^{-1} \right] \right|^{-1}$$

 $\alpha(\mathbf{q}) \geq \beta(\mathbf{q})$  and  $\beta(\mathbf{q}) \geq \gamma(\mathbf{q})$  are the eigen values of the deformation tensor

$$d_{ik}(\mathbf{q}) = \frac{\partial s_i}{\partial q_k} = -\frac{\partial^2 \Phi}{\partial q_i \partial q_k}$$

Linear density fluctuations:  $\delta \rho / \rho = D(t)(\alpha + \beta + \gamma).$ 

The Zel'dovich approximation describes anisotropic collapse and motion.



Hidding, Shandarin, van de Weygaert 2014

Assumptions are not realistic, approximation is kinematic, pancakes are unstable therefore no observable traces

### Lagrangian Submanifold (LS) is N-dim surface in 2N-dim space





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### State of art N-body simulations



Figure 1. X-Y projection of the particle positions for a 20000-body numerical experiment after the system has expanded by a factor of 9.9. In this case the expansion follows that of an Einstein-de Sitter model,  $\Omega_0 = 1.0$ .

**1981** Efstathiou, Eastwood, MNRAS, 194, 503



**1979** Aarseth, Gott, Turnet, Astrophys. J. 228, 644

Structure predicted by "Zeldovich Approximation" aka "Pancake model"

Published in a review paper by Doroshkevich, Zeldovich, Sunyaev 1976 (only in Russian)

Caption says: "the figure is made by S. Shandarin"

and also by Doroshkevich and Shandarin, 1978 Sov.Astron. 22(6), 653



Figure 1. Examples of the general patterns arising in twodimensional models. The dark regions are regions of three streams flows. a) 'pancake', b) and c) two types of merging of pancakes. Solid lines are caustics - lines of infinite density.

### Shandarin in

The Origin and Evolution of Galaxies: Proceedings of the NATO Advanced Study Institute held at Erice, Italy, May 11–23, 1981. VII-th Course of the ... and Gravitation (Nato Science Series C:) Hardcover – December 31, 1982 page 171



Figure 3. An example of the structures arising in 3D numerical simulations of the adiabatic scenario. The surface is a surface of constant density  $\rho \sim 2.5 \rho$ .

### State of art N-body simulations **1981** Efstathiou, Eastwood, MNRAS, 194, 503

Clustering of particles in an expanding Universe



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*Figure 12* "Wedge diagram" of the Coma supercluster [Gregory & Thompson (40)]. As the supercluster is elongated in the east-west direction, right ascensions have been chosen as position coordinates; the galaxies lie between  $+19^{\circ}$  and  $+32^{\circ}$  declination. The angular size has been magnified about two times compared with the indicated distance scale.

Gregory & Thompson 1978 see also Chincarini & Rood 1976

### de Vaucouleurs 1981

Tully 82





Figure 3 All 2175 galaxies in the Nearby Galaxy Catalog (NBG) projected onto the SGY-SGZ plane. The SGY-axis is directed toward supergalactic longitude 90°, supergalactic latitude 0° ( $\ell^{II} = 227^{\circ}$ ,  $b^{II} = +83^{\circ}$ ?), the SGZ-axis toward supergalactic latitude 90° ( $\ell^{II} = 47^{\circ}$ .4,  $b^{II} = +6^{\circ}$ .3). The radius of the outer boundary is 60 Mpc. The galactic zone of avoidance ( $b < 15^{\circ}$ ) is contained within the opposed wedges tilted by 6° with respect to the SGZ-axis. There is a zone of incompletion ( $\delta < -45^{\circ}$ ), which is projected across most of the southern supergalactic hemisphere. Figures 3–6 are reproduced by courtesy of R. B. Tully (92).

Figure 2. Distribution of the Shapley-Ames galaxies (1932) in (old) galactic coordinates. The zone of avoidance (dark) and of partial obscuration (grey) by the Milky Way is indicated. The super-galactic equator and parallels at  $\pm 30^{\circ}$  latitude are marked. Two external galaxy clouds in Hydra  $(l^{I} = 240^{\circ})$  and Pavo-Indus  $(l^{I} = 310^{\circ})$  and the elongated Dorado-Fornax-Eridanus stream or "southern supergalaxy" are cutlined.



Below is the image in its original context on the page: www.astro.princeton.edu/ ~mjuric/universe/



Three-dimensional DTFE reconstruction of the inner parts of the 2dF Galaxy Redshift Survey

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Flip-Flop on particles: change of sign of  $det \left[ \partial x_i / \partial q_k \right]$ 

#### Flip-Flop field in Lagrangian space in 1024<sup>2</sup> simulation





a=2.3

density field

a=3.4

a=59



Figure 2. Evolution of structure in two-dimensional N-body simulation. Four stages are shown at  $a \approx 1.0$ , 2.3, 3.4 and 58.7 from top to bottom. The density perturbation linearly extrapolated would result in  $\delta_{\rm rms} = 1$  at a = 1. The CIC density fields in Eulerian space are shown in the left column. The corresponding

#### flip-flop field

#### **3** N-BODY SIMULATIONS

The initial conditions were generated with NGenIC code<sup>4</sup> with the standard  $\Lambda$  cold dark matter ( $\Lambda$ CDM) cosmology,  $\Omega_m =$ 0.3,  $\Omega_{\Lambda} = 0.7$ ,  $\Omega_b = 0$ ,  $\sigma_8 = 0.9$ , h = 0.7 and the initial redshift z = 50. A set of simulations were carried out with a box  $1 h^{-1}$  Mpc and total mass  $M_{b,dm} \approx 1.2 \times 10^{11} \text{ M}_{\odot}$ . For illustration purposes, we present two simulations with  $128^3$ ,  $m_{part} \approx 5.7 \times 10^4 \text{ M}_{\odot}$  and  $256^3$ ,  $m_{part} \approx 7.1 \times 10^3 \text{ M}_{\odot}$  DM particles with the force resolution of  $1.5 h^{-1}$  and  $0.75 h^{-1}$  kpc respectively. The chosen size of the box is obviously too small for the purpose of deriving statistically valid

Table 1. Number of particles in substructures shown in Fig. 22									
flip-flop threshold	$N_1$	$N_2$	$N_3$	$N_4$	$N_5$	$N_6$	$N_7$		
100	206670								
150	61960	17035	513	308	265				
240	8698	3960	211						
270	4363	1474	753	521					
300	1976	416	405	381	286	267	178		

Table 2. Approximate masses of substructures shown in Fig. 22 in units of  $10^6 M_{\odot}$ 

flip-flop threshold	$M_1$	$M_2$	$M_3$	$M_4$	$M_5$	$M_6$	$M_7$
100 150 240 270 300	$1464. \\ 439. \\ 61.6 \\ 30.9 \\ 14.0$	121. 28.1 10.4 2.94	3.63 1.50 5.34 2.87	2.18 3.70 2.70	1.87 2.03	1.89	1.26



**Figure 22.** The marching cubes isosurfaces of the flip-flop field show five levels of hierarchical structure of the largest flip-flop peak in the  $256^3$  simulation in Lagrangian space. All panels show the surface of the peak





### "Phase space" (kpc, km/s)





### Lagrangian Space

### "Phase space" at z=0



levels of hierarchical structure of the largest flip-flop peak in the  $256^3$  simulation in Lagrangian space. All panels show the surface of the peak



**Figure 12.** Correlation coefficient of the density  $\xi_{\rho \cdot \rho}$  (red), potential  $\xi_{\varphi \cdot \varphi}$  (blue) and flip-flop  $\xi_{\text{ff} \cdot \text{ff}}$  fields at a = 1 (long curves) and a = 0.1 (short curves) with corresponding fields at all previous stages. In order to see how close to unity  $\xi_{\text{ff} \cdot \text{ff}}$  is, we plot the logarithm of its difference from unity. The curves are shown for both  $N_p = 128$  (triangles) and 256 (circles) simulations.



Vertical: mean(n\_ff) in top; std(n\_ff)) in bottom in fraction on the right ;

$$n_{ff}(t + \Delta t) = n_{ff}(t) + \Delta n_{ff}(\Delta t)$$

*The rich get richer and the poor get poorer* 

$$\rho(r) \propto r^{-n}$$
$$t \propto r^{n/2}$$



**Figure 14.** Conditional statistics of the flip-flop field as a function of the scalefactor. The particles are binned according to the change of the number of flip-flops between the outputs  $\Delta_{\text{ff}} = n_{\text{ff}}(a_{i+1}) - n_{\text{ff}}(a_i)$ . The curves are in the range  $0 \le \Delta_{\text{ff}} \le 12$  from the bottom to top in top two panels and in the reverse order in the bottom panel. The panels show the mean, std and fraction of the particles in each bin from top to bottom.

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#### x = q - t sin q

### Phase space



#### Dashed lines show previous stage

#### Density





#### Phase space

## Lagrangian submanifold q(x) or x(q)

q(x) is multi valued (one-to-many) x(q) is single valued (one-to-one)

Density (gray, filled) V.S. number of streams (red line) Shandarin, Habib, Heitmann 2011 subm. 9 Nov. The Middle tetrahedra Abel, Hahn, Kaehler 2011 subm. 16 Nov. Figure 1.9: The Tetrahedra orientation within a cube DENSITY **FIELD MULTI-STREAM FIELD** 

Fields are computed on a uniform 3D diagnostic grid in configuration space by projecting tetrahedra from 6D to 3D.The refinement of 3D diagnostic grid is increasing from left to right (1, 4, 16) The distribution of particles remains the same in all plots.

### All halos are embedded in filaments

Ramachandra, Shandarin, MNRAS, 467, 1748, 2017



streams

density



streams

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#### **Tracing the Cosmic Web**<sup>\*</sup>

Noam I Libeskind<sup>1</sup><sup>†</sup>, Rien van de Weygaert<sup>2</sup>, Marius Cautun<sup>3</sup>, Bridget Falck<sup>4</sup>, Elmo Tempel<sup>1,5</sup>, Tom Abel<sup>6,7</sup>, Mehmet Alpaslan<sup>8</sup>, Miguel A. Aragón-Calvo<sup>9</sup>, Jaime E. Forero-Romero<sup>10</sup>, Roberto Gonzalez<sup>11,12</sup>, Stefan Gottlöber<sup>1</sup>, Oliver Hahn<sup>13</sup>, Wojciech A. Hellwing<sup>14,15</sup>, Yehuda Hoffman<sup>16</sup>, Bernard J. T. Jones<sup>2</sup>, Francisco Kitaura<sup>17,18</sup>, Alexander Knebe<sup>19,20</sup>, Serena Manti<sup>21</sup>, Mark Neyrinck<sup>3</sup>, Sebastián E. Nuza<sup>22,23,1</sup>, Nelson Padilla<sup>11,12</sup>, Erwin Platen<sup>2</sup>, <u>Nesar Ramachandra<sup>24</sup></u>, Aaron Robotham<sup>25</sup>, Enn Saar<sup>5</sup>, <u>Sergei Shandarin<sup>24</sup></u>, Matthias Steinmetz<sup>1</sup>, Radu S. Stoica<sup>26,27</sup>, Thierry Sousbie<sup>28</sup>, Gustavo Yepes<sup>18</sup>

Affiliations are listed at the end of the paper

10 May 2017

#### TEST DATA: SIMULATION AND DATA SET

Each of the participants applied their web identification methods to the same Gadget-2 (Springel 2005) dark matter only *N*- body simulation,

with a box size of 200  $h^{-1}$ Mpc and 512<sup>3</sup> particles.

The  $\Lambda$ CDM cosmological parameters are taken from Planck (Planck Collaboration et al. 2014): h = 0.68,  $\Omega M = 0.31$ ,  $\Omega \Lambda = 0.69$ ,  $n_s = 0.96$ , and  $\sigma 8 = 0.82$ .

Haloes in the simulation are identified using a standard FOF algorithm (Davis et al. 1985), with a linking length of b = 0.2 and a minimum of 20 particles per halo.



Figure 1. A thin slice through the cosmological simulation used for comparing the web identification methods. The left panel shows the density field in a  $2 h^{-1}$ Mpc slice with darker colours corresponding to higher density regions. The red lines show the  $\delta = 0$  contours (dividing over and under dense regions, with respect to the mean) and are reproduced in the right panel (and in Fig. 2 as black lines). The right panel shows the positions of haloes in a  $10 h^{-1}$ Mpc slice, where symbol sizes are scaled by halo mass. This same slice will be used to showcase the web identification methods in Figs. 2 and 3 as well as the level of agreement across web finders in Fig. 7.

# N. R. S. Sh.

MSWA= MultiStream Web Analysis





![](_page_50_Figure_0.jpeg)

Figure 5. The mass and volume filling fraction of knots (top-left), filaments (top-right), sheets (bottom-left) and voids (bottom-right) as identified by the various cosmic web finders. These quantities were computed using a regular grid with a cell spacing of 2  $h^{-1}$ Mpc. The solid line shows the mean filling fraction, i.e. a slope of unity, where the volume filling fraction equals the mass filling fraction. Namely, points above this line lie in under-densities, points below it in over-densities.

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![](_page_52_Figure_0.jpeg)

![](_page_52_Figure_1.jpeg)

![](_page_53_Figure_0.jpeg)

Figure 1. Examples of the general patterns arising in twodimensional models. The dark regions are regions of three streams flows. a) 'pancake', b) and c) two types of merging of pancakes. Solid lines are caustics - lines of infinite density. Caustics in Zeldovich Approximation Hidding, Shandarin, van de Weygaert 2014

Caustics in 2D

Red – Lam\_1 Blue – Lam\_2

#### Caustics in 3D

![](_page_54_Figure_4.jpeg)

#### Arnold 1982

![](_page_55_Figure_1.jpeg)

Caustics in 3D N-body simulations: triangle interface between neighboring tetrahedra  $V_1 > 0$  and  $V_2 < 0$ 

![](_page_56_Picture_1.jpeg)

## Summary

#### DM Web

New fields: number of streams and flip-flop fields, and caustic surfaces reveal new properties of the cosmic web. All are easy to compute from standard cosmological simulations, however require the tessellation of the initial state.

The dark matter web is defined as the part of the universe where the number of streams greater than one. It spans throughout the entire volume of the universe occupying about 10% of the volume.

The void regions occupy the rest 90% of the volume. The largest percolating void occupy about 99% of all the single-streaming regions. (A sponge topology)

The number of flip-flops as a function of Lagrangian coordinate stores information about the merging history of DM halos.

The volume and mass fractions in voids measured by MSWA=Multi Stream Web Analysis are the largest (0.90 and 0.56 respectively) of all measured by other methods in the comparison project.