

- Random data Cauchy theory for nonlinear wave equations
 - ▶ **Guiding question:** What is the generic behaviour of solutions of a given PDE with rough and random initial data?
 - ▶ low regularity well-posedness for random initial data
 - ▶ asymptotic behaviour of these random solutions, e.g. scattering
- Infinite dimensional Hamiltonian systems, symplectic non-squeezing
 - ▶ **Guiding question:** which features of finite dimensional Hamiltonian equations carry over to infinite dimensions and what can they tell us about the behaviour of solutions to these Hamiltonian PDEs?