

# The mathematics of imaging: the CIRM pre-school

## An adaptive watershed by flooding algorithm for an atlas of brain parcellations.

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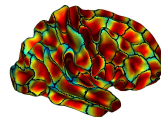
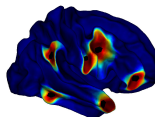
Collaborators: C. Deruelle, L. Brun, J. Lefèvre, O. Coulon, and G. Auzias

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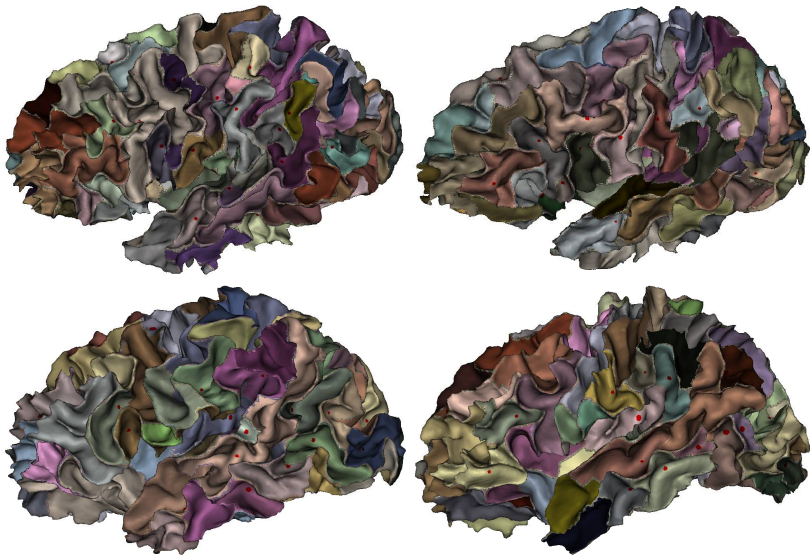
Adaptive watershed by flooding

From local maps



to global parcelling

## Variability of the cortical surface



# Cortical folding

## 1. Cortical folds :

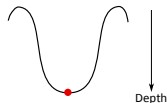
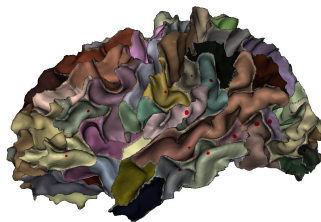
- ▶ Name : *sulcus* (pl. *sulci*)
- ▶ Common organization
- ▶ Highly variable geometry and topology

## 2. Sulcal basins :

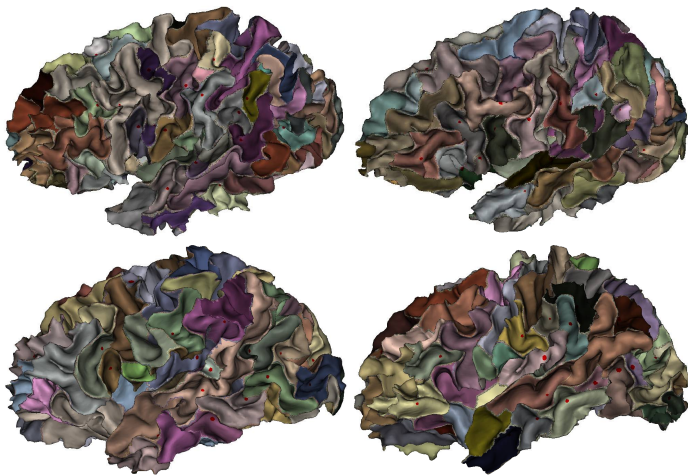
- ▶ Subdivisions of the sulci
- ▶ 1 sulcal pit in each basin

## 3. Sulcal pits :

- ▶ **Robust landmark**
- ▶ Point of maximal depth in each basin →
- ▶  $100 \pm 5$  pits by subject



## How to establish the correspondences between these parcels ?

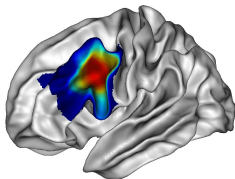
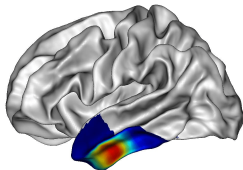
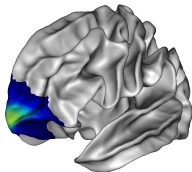


and how to build an atlas parcellation in order to

- ▶ define a nomenclature of the sulcal basins
- ▶ have an insight on the average shape of these basins



## Heuristic to build an atlas of sulcal basins

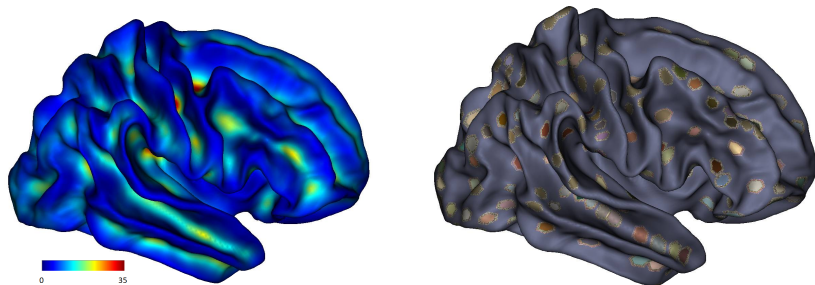


**After registration**, the density maps of homologous sulcal basins contain the geometry of these basins. These maps require yet to identify these basins across the population.

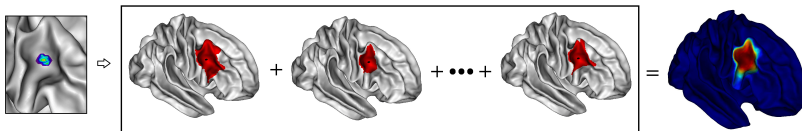
**Aim:** to jointly **build an atlas** map of sulcal basins and to **identify individual basins** with respect to this atlas.

**Method:** a watershed by flooding algorithm on the density maps of sulcal basins.

## Initialization of the clusters

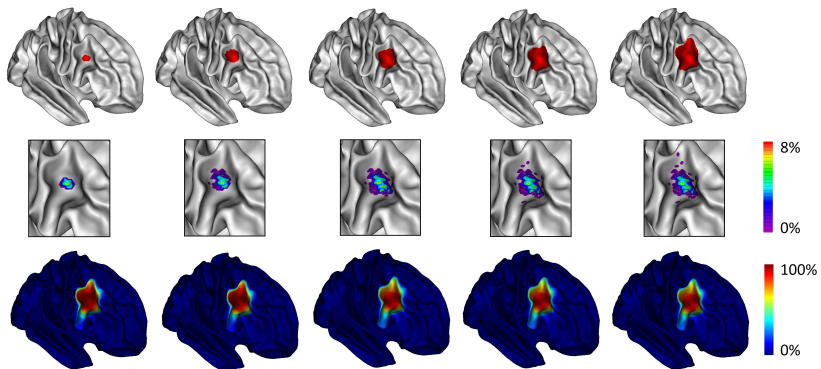


Density map of sulcal pits and clusters initialized with a small neighborhood around the maximums of the density map.

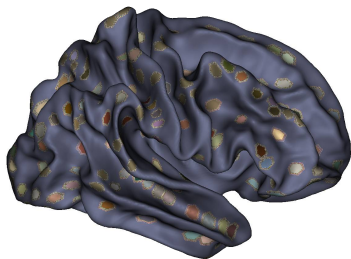


Identification of the first sulcal pits and extraction of associated sulcal basins.

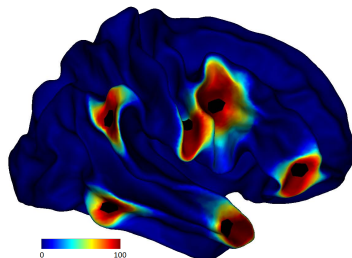
## Growing cluster and learning of the influence map



## Some initial influence maps

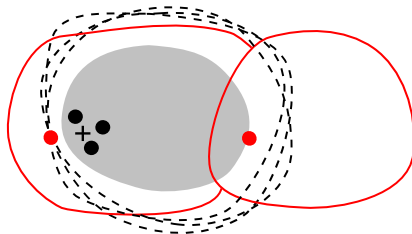


Initial clusters.



Some estimated **normalized density maps of sulcal basins**, called **influence maps**, (merged in one texture) with their respective **cluster in black**.

## Improved learning of the influence maps



In order to improve the **robustness of these influence maps**, we filter the new pits assigned to a cluster according to a **geometrical criterion**:

- ▶ a new basin candidate (e.g. right red basin) must contain the seed "+" of the cluster (its first vertex)

This also ensures labeling uniqueness for each subject !

## Clusters' filtering

**The irregularity of the density map of sulcal pits produces too many seeds: we have about 170 clusters when subjects have about 100 sulcal basins.**

Underlying minimization problem:

$$\min_{(N, C, \gamma)} \sum_{\text{subject } i} \sum_{k \in \text{Def}(\gamma_i)} d(B_i(\gamma_i(k)), C(k))^2 + \lambda \sum_{j \notin \text{Im}(\gamma_i)} \ell(B_i(j))$$

where the unknown variables are

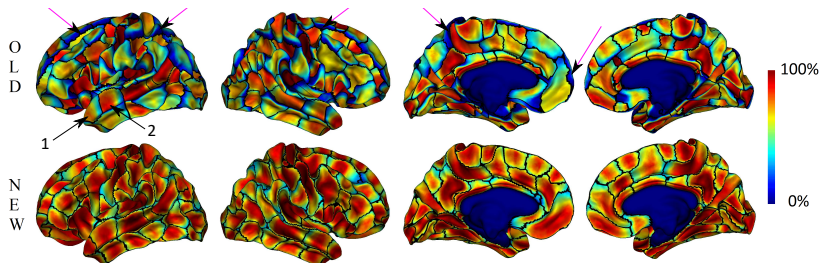
- ▶ the number of clusters  $N > 0$
- ▶ the shape of these clusters  $C$
- ▶ the mappings  $\gamma$  between clusters and individual sulcal basins

and where  $d$  measures the similarity between the individual basins and the clusters and  $\ell$  penalizes the rejected individual basins.

**$\lambda$  defines the trade-off between matching accuracy and the number of unlabeled sulcal basins. It regulates the flexibility of the model with respect to minor patterns of sulcal basins.**

In practice: we iteratively delete the clusters that induce the smallest pits lost with a stop criterion grounded on the minimal % of subjects associated to each cluster.

## Results on 137 adults: comparison with a clustering method on sulcal pits

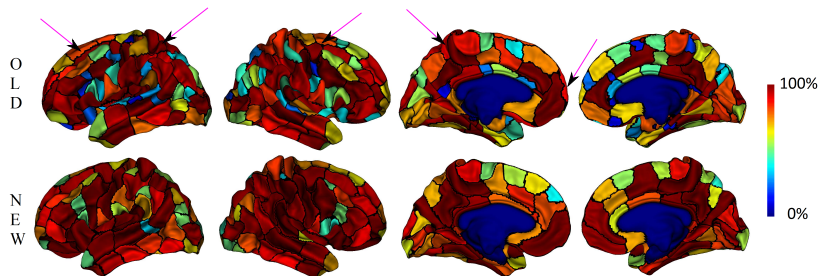


**Merged influence maps** for the old pipeline (first row) and new pipeline (second row).

For more details, see

I. Kaltenmark, G. Auzias, L. Brun, J. Lefèvre, C. Deruelle, and O. Coulon. Cortical inter-subject correspondences with optimal group-wise parcellation and sulcal pits labeling, (*available on Hal*).

## Results on 137 adults: frequency in each cluster



**Final  $N_1$  scores, percentage of subjects that have a pit associated to a given cluster.** First row: old method. Second row: new method.