# Habitat quality and the velocity of spatial population expansion

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#### Planet at the crossroads

www.iucnworldconservationcongress.org 1-10 September 2016, Hawai'i





#### Planet at the crossroads

www.iucnworldconservationcongress.org 1-10 September 2016, Hawai'i



Photo Martha de Jong-Lantink



#### Endangered (2008)



#### Planet at the crossroads

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#### Vulnerable (2016)



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#### Photo Martha de Jong-Lantink

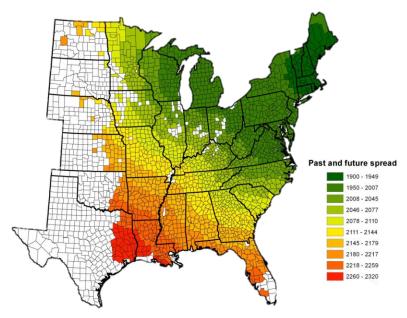


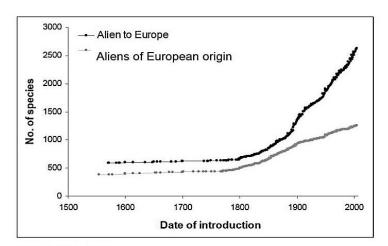
#### Vulnerable (2016)



# **Biological invasion**

- 2nd cause of biodiversity loss (IUCN)
- 12 billions Euros per year in Europe (Kettunen et al., 2009)





Source: DAISIE project

Past and predicted future spread of the gypsy moth Epanchin-Niell &Liebhold 2015

# Habitat quality and the velocity of spatial population expansion

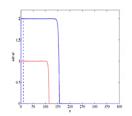
How the quality of the landscape can affect the spreading velocity?

Proxy of habitat quality = Carrying capacity

Carrying capacity (K) : Maximum number of individuals an area can support

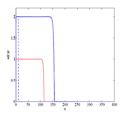
## **Studied Mechanisms**

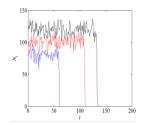
- (1) Classic model (Fisher-KPP)
- (2) Positive density dependent dispersal (DD dispersal)
- (3) Positive density dependent growth (strong Allee effect)
  - -> Reaction-Diffusion Models



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- (4) Stochasticity {Fisher-KPP, DD dispersal, Allee effect}
  - -> Individual Based Model

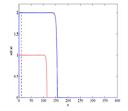


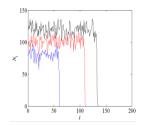


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(1) Classic model (Fisher-KPP)

Equation:  $\frac{\partial u}{\partial t} = D \frac{\partial^2 u}{\partial x^2} + ru(1-u)$ 

Velocity Formulae :

$$v = 2\sqrt{rD}$$

(1) Classic model (Fisher-KPP)

Equation : 
$$\frac{\partial u}{\partial t} = D \frac{\partial^2 u}{\partial x^2} + ru \left(1 - \frac{u}{K}\right)$$

$$v = 2\sqrt{rD}$$

#### => Constant velocity whatever K

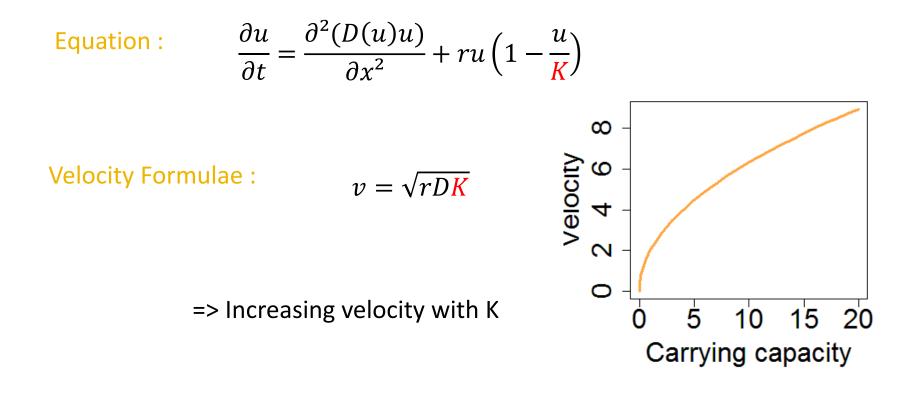
(2) Positive density dependent dispersal (DD dispersal)

Equation: 
$$\frac{\partial u}{\partial t} = \frac{\partial^2 (D(u)u)}{\partial x^2} + ru(1-u)$$

$$D(u) = u^a$$

with a >

(2) Positive density dependent dispersal (DD dispersal)



(3) Positive density dependent growth (Allee effect)

Equation: 
$$\frac{\partial u}{\partial t} = D \frac{\partial^2 u}{\partial x^2} + ru(1-u)(u-\rho)$$

 $\rho$  = Allee threshold

(3) Positive density dependent growth (Allee effect)

Equation:  

$$\frac{\partial u}{\partial t} = D \frac{\partial^2 u}{\partial x^2} + ru \left(1 - \frac{u}{K}\right) (u - \rho)$$
Velocity Formulae:  

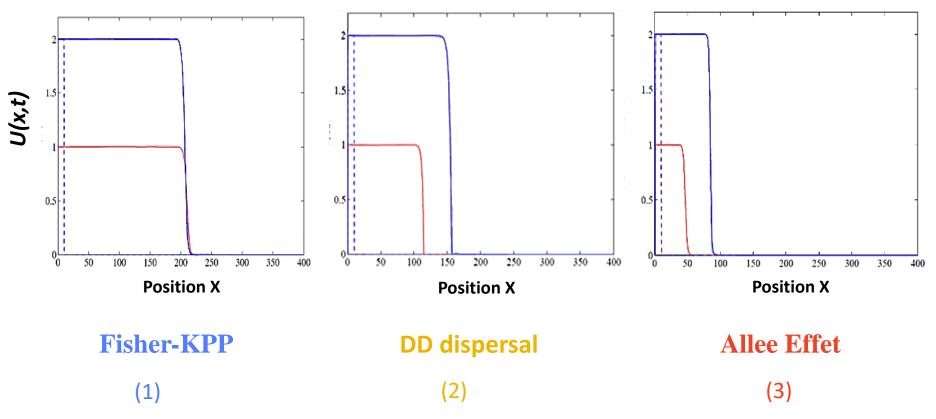
$$v = \sqrt{\frac{2rD}{K}} \left(\frac{K}{2} - \rho\right)$$

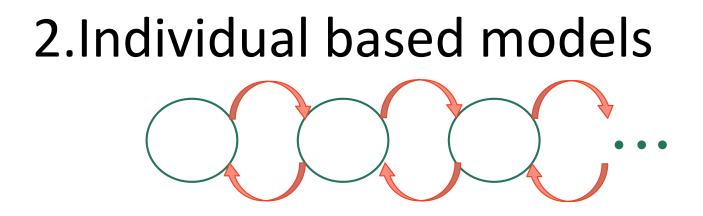
$$\stackrel{\text{Or}}{=} \int_{0}^{0} \int_{0}^{1} \int_{$$

- Travelling waves for
  - *K*=1 (red)

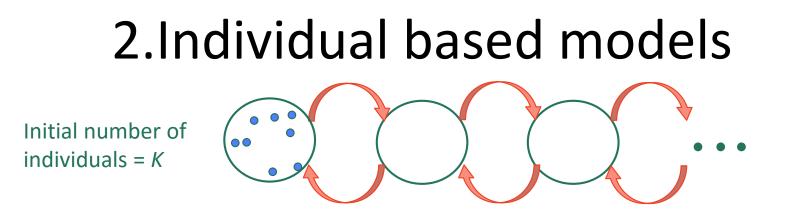
T = 100

- K=2 (blue)

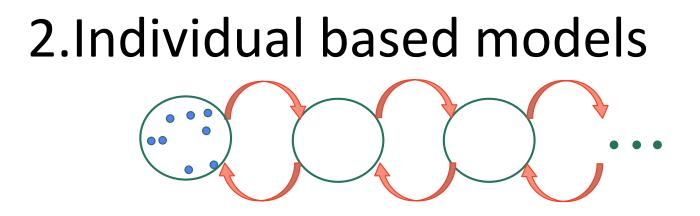




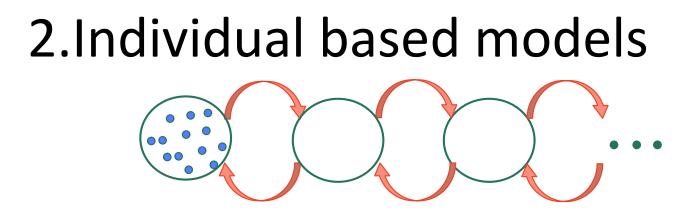
Discrete space: stepping stone landscape



- Discrete space: stepping stone landscape
- Discrete state: population size in number of individuals

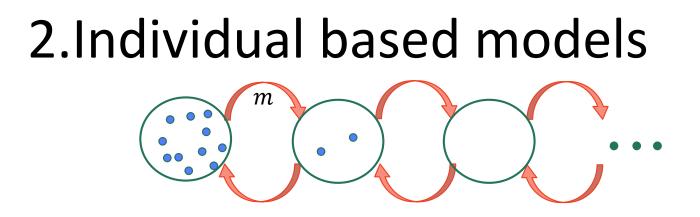


- Discrete space: stepping stone landscape
- Discrete state: population size in number of individuals
- Discrete time: non overlapping generations



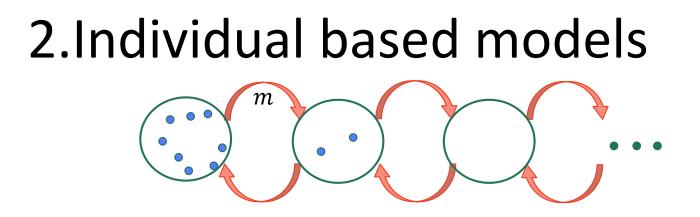
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• Reproduction (Poisson process)



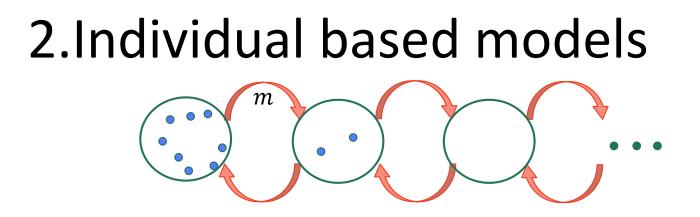
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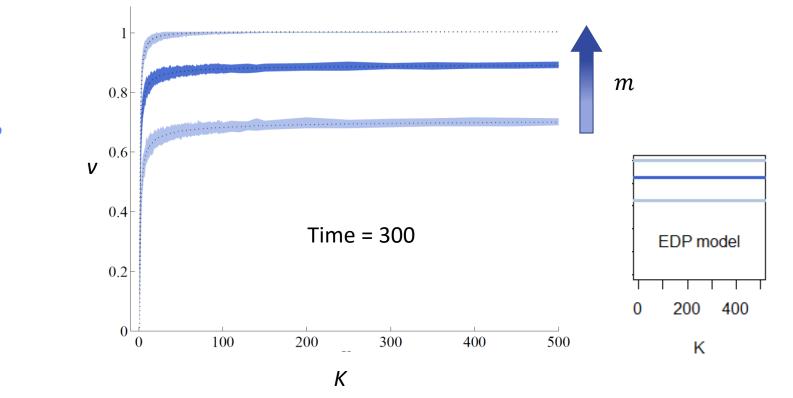
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3 scenarios: Fisher-KPP, DD dispersal, Allee effect

v for K  $\in$  [1:500], 200 replicated simulations. 99% conf. int.

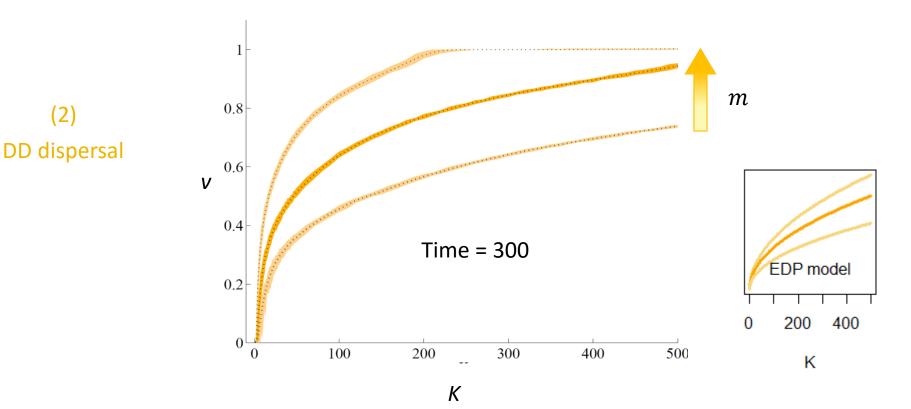
Probability to disperse:  $m = \{0.25, 0.5, 0.75\}$ 



(1) Fisher-KPP

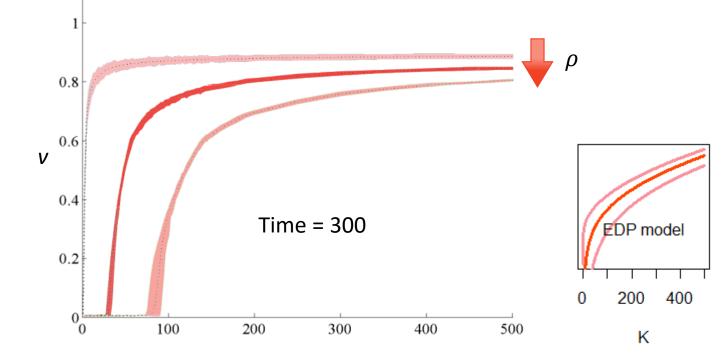
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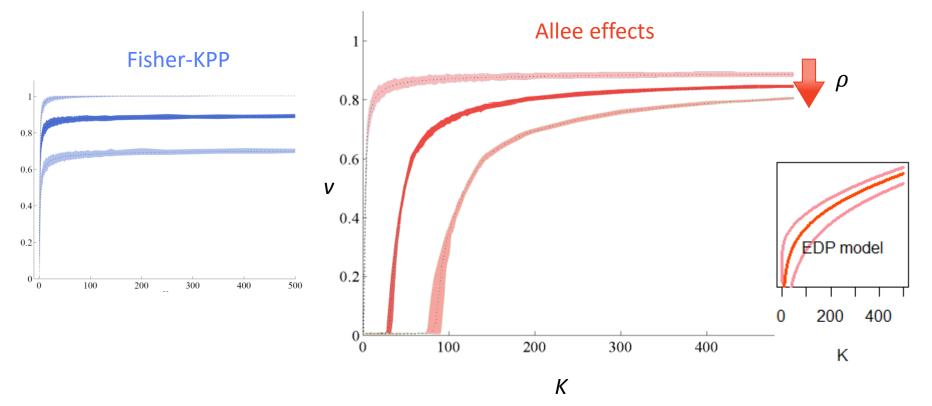
Probability to disperse : m = 0.5Allee threshold:  $\rho = \{1, 20, 50\}$ 



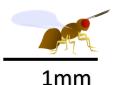
(3) Allee effects

v for K  $\in$  [1:500], 200 replicated simulations. 99% conf. int.

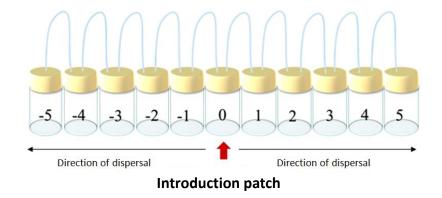
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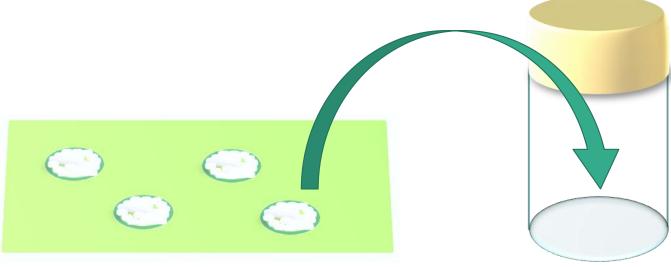
- Biological model: minute wasp, *Trichogramma chilonis* 
  - small size, short generation time
  - tendency to positive DD dispersal (scenario 3)



Environment: Linear landscape in stepping stone



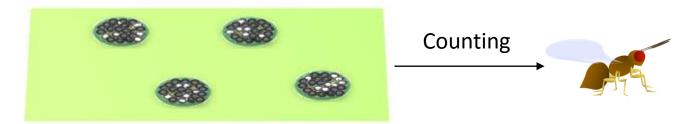
- Biological model:
  - Parasitoid
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  - One piece of paper (=K) by patch



- Biological model:
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  - One piece of paper (=K) by patch
  - Parasitized eggs turn dark



• Biological model: *Trichogramma chilonis* 



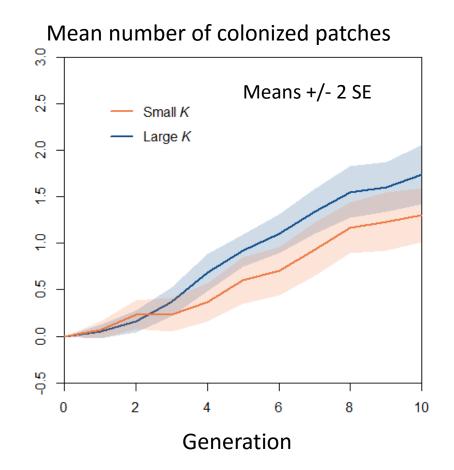
 2 modalities of carrying capacity: Small: ~ 150-200 host eggs Large: ~400-450 host eggs

x20 Replicats x20 Replicats

• 10 generations = 99 days

Statistical analysis General Linear Mixed Model :

Is there any difference in the mean number of colonized patches between the two modalities of carrying capacity?

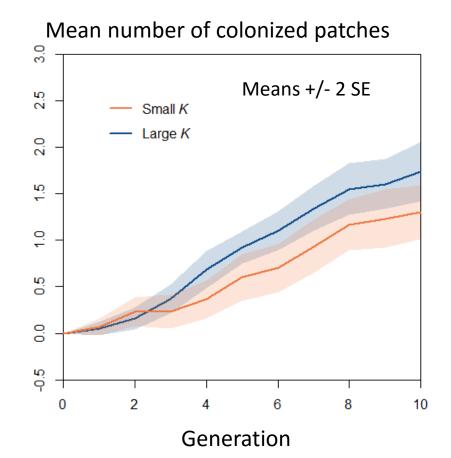


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Z-value = 2.008 p\_value = 0.0447

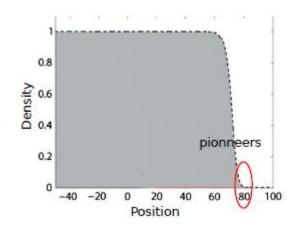
Small K: + 0.13 patch per generation Large K: + 0.17 patch per generation



- carrying capacity impact on spreading speed was overlooked
- Different mechanisms may lead populations to have a spreading speed positively influenced by habitat quality:
  - positive density dependent migration
  - positive density dependent growth (Allee Effect)
  - stochasticity (small populations)
- Marginal influence of K decreases with K (may vanish for large K)
- Large scale may hide K/v relation
- Relationship K/v -> indicator of pushed waves?

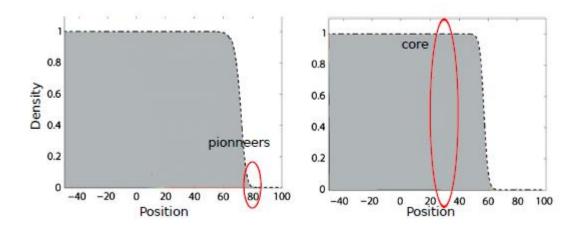
Relationship K/v -> indicator of pulled/pushed nature of the expanding front ?

 Propagation speed depends on the growth function for small population densities in the edge -> Fisher-KPP (pulled wave)



Relationship K/v -> indicator of pulled/pushed nature of the expanding front ?

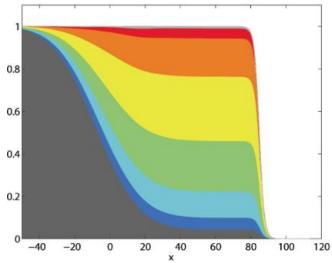
- Propagation speed depends on the growth function for small population densities in the edge -> Fisher-KPP (pulled wave)
- Propagation speed depends on the growth function of the core population -> Allee effect (Pushed wave)



Relationship  $K/v \rightarrow$  indicator of pulled/pushed nature of the expanding front?

Roques & al. 2012: Allee effect promotes diversity in traveling waves of colonization

Pulled



Pushed

0.8

0.6

0.4

0.2

0

-20

0

20

40

x

60

80

100



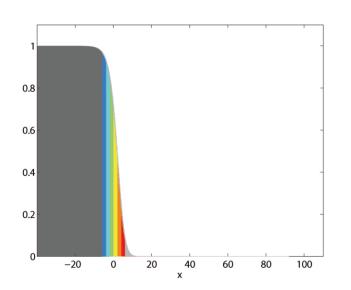
#### Thank you for listening!

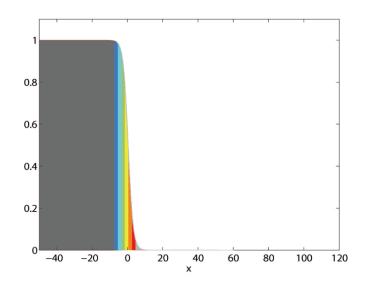


Trichogramma having fun with waves

A link between *K*-speed and the pulled/pushed nature of the expanding front ?

Roques & al. 2012: Allee effect promotes diversity in traveling waves of colonization





Pulled

Pushed