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## Latent heat and heat conduction

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It is from a joint work with Matteo Colangeli and Anna De Masi.

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Construction of metastable states with a non-zero current and no external forces.



Figure: Magnetization profiles for C = 1.25 and  $m_+ = 1$  with space in  $\gamma^{-1}$  (= 30) units. The parameters  $m_\beta$  and  $m^*$  have values  $m_\beta = 0.985$  and  $m^* = 0.885$ . The different curves in the plot correspond to the averaged magnetization computed at different times:  $t = 10^5$  (green curve),  $t = 10^6$  (orange curve),  $t = 10^7$  (purple curve) and  $t = 10^8$  (blue curve). The red curve denotes the initial configuration.



Figure: Magnetization profiles for C = 0,  $m_{\beta} = 0.985$  and  $m^* = 0.885$ , and with  $m_+ = 0.93$ . The curves in the plot have the same meaning of those illustrated in Fig. 1. The standard Fourier law is satisfied.



Figure: Magnetization profiles for C = 1.25,  $m_{\beta} = 0.985$  and  $m^* = 0.885$ , and with  $m_+ = 0.93$ . The curves in the plot have the same meaning of those illustrated in Fig. 1.



Figure: Schematization of the system made of two reservoirs R1 and R2, endowed with magnetization  $m_-$  and, respectively,  $m_+$  and connected by two channels. The channel on the top (blue arrow) is characterized by C > 0.5, hence the current flows from the smaller density corresponding to  $m_-$  to the larger one corresponding to  $m_+$ , cf. Fig. 3. The channel on the bottom (black arrow) has C = 0 and the corresponding current flows in the opposite direction, cf. Fig. 2.



Figure: Values of the current for different values of the exchange rate between finite reservoirs



Figure: Magnetization profile when the infinite reservoirs impose magnetization  $\boldsymbol{0}$