Dorin Popescu: On the regular local rings.

R. Swan asked if a regular local ring is a filtered inductive limit of regular local rings essentially of finite type over Z. We showed that this holds for regular local rings (A, m, k) which are in one of the following cases:

i) A contains a field,

ii) the characteristic p of k is not in m^2 ,

iii) A is excellent Henselian (the proof in this case uses the Artin approximation property).

This result has consequences concerning a question of Quillen and the Bass-Quillen conjecture.