Joël Nagloo: On the non-generic Second Painlevé equation..

In this talk we will look at the problem of existence of algebraic relations over $\mathbb{C}(t)$ between solutions of the second Painlevé equation $P_{II}(\alpha)$: $y'' = 2y3 + ty + \alpha$ for algebraic $\alpha \notin 1/2 + \mathbb{Z}$. In particular, I will discuss recent progress in showing that if y_1, \ldots, y_n are distinct solutions, then $tr.deg(\mathbb{C}(t)(y_1, y'_1, \ldots, y_n, y'_n)/\mathbb{C}(t)) = 2n$, that is $y_1, y'_1, \ldots, y_n, y'_n$ are algebraically independent over $\mathbb{C}(t)$.